

# **SPY: a microscopic statistical scission-point model to predict fission fragment distributions**

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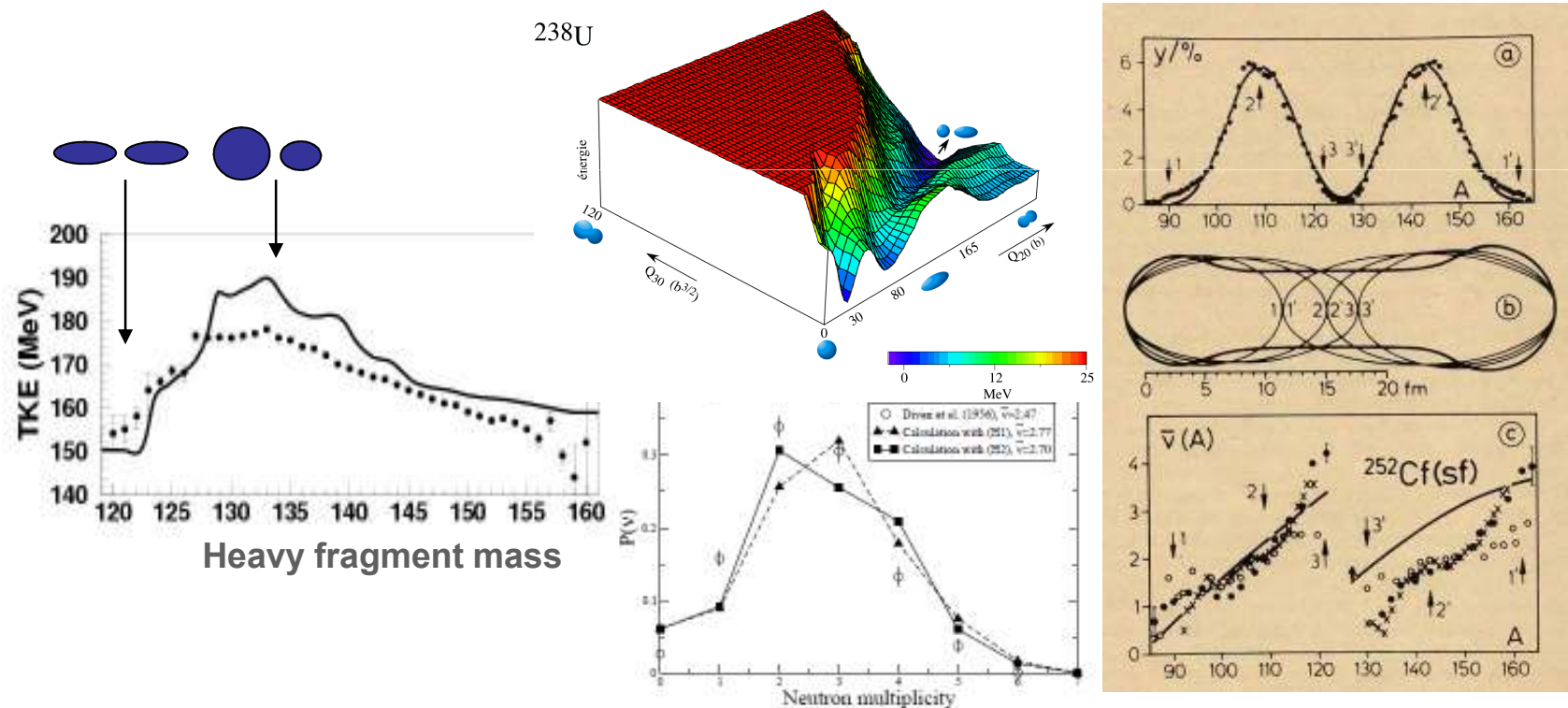
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***3rd Workshop on Nuclear Density and Gamma  
Strenght – Oslo, 23-27 May 2011***

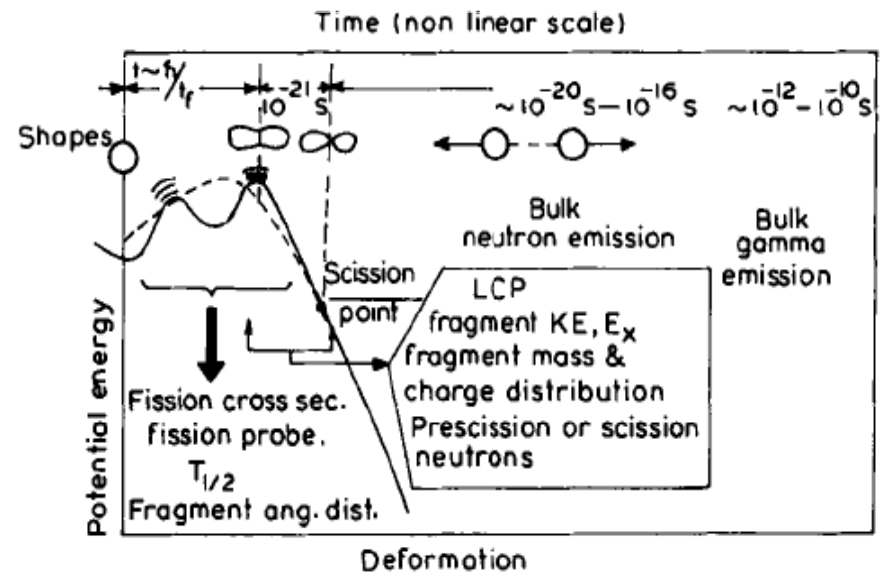
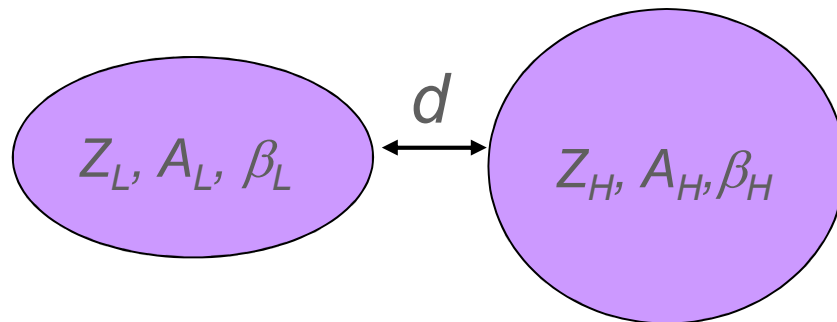
# Fission: an old reaction over towards new challenges

- The fission process is the most complete nuclear physics laboratory
  - Internal nuclear structure (shell effects, pairing,...)
  - Nuclear deformations
  - Dynamics (coupling between collective modes and internal excitation)
- A lot of data and models to interpret them but still...



# The scission-point model

- First proposed by Wilkins (*Wilkins et al, Phys. Rev. C 14 (1976) 5*)
- **Static approach:**
  - Fission process is slow
  - A **statistical «quasi»-equilibrium** is reached at scission
  - The main fragment characteristics are frozen at this point!
  - Dynamics is not explicitly treated
  - The scission configuration is defined by **two ellipsoids** with an inter-surface **distance d**

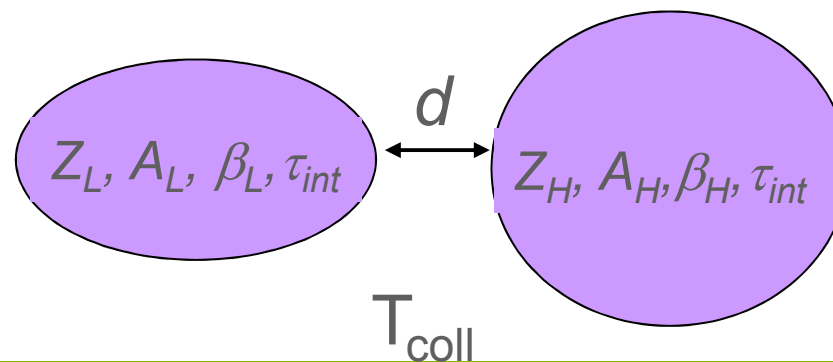


# The scission-point model

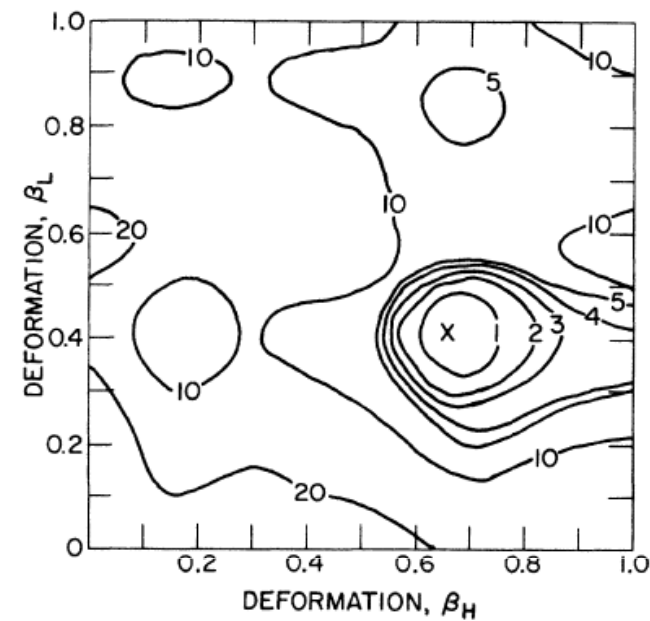
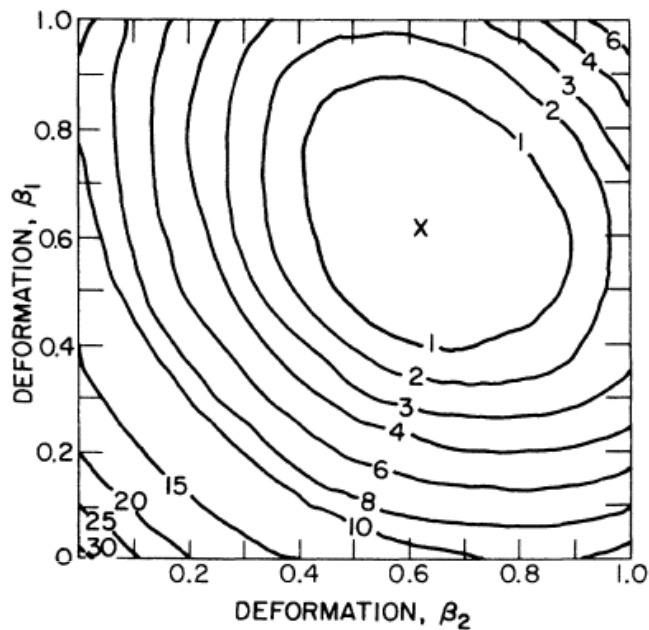
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- First proposed by Wilkins (*Wilkins et al, Phys. Rev. C 14 (1976) 5*)
- Static approach
- Based on an **energy balance at scission**
- Main **limitations**:
  - Collective and intrinsic temperature parameters (+ d!) fitted on data
  - Energy potentials are relative to the scission point
  - Only prolate deformations
  - Individual energies are not microscopic (liquid drop + Strutinski + pairing)

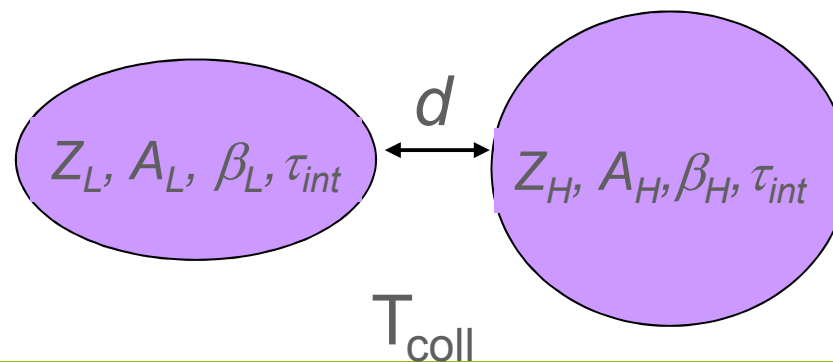
$$V(Z_{1,2}, N_{1,2}, \beta_{1,2}, d, \tau_{1,2}) = \Sigma V_{LD}^{1,2}(Z^{1,2}, N^{1,2}, \beta^{1,2}) + \Sigma V_{Str.}^{1,2}(Z^{1,2}, N^{1,2}, \beta^{1,2}, \tau_{1,2}) \\ + V_{coul}(Z_{1,2}, N_{1,2}, \beta_{1,2}, d) + V_{nucl}(Z_{1,2}, N_{1,2}, \beta_{1,2}, d)$$



# The scission-point model: Wilkins



$$V(Z_{1,2}, N_{1,2}, \beta_{1,2}, d, \tau_{1,2}) = \Sigma V_{LD}^{1,2}(Z^{1,2}, N^{1,2}, \beta^{1,2}) + \Sigma V_{Str.}^{1,2}(Z^{1,2}, N^{1,2}, \beta^{1,2}, \tau_{1,2}) + V_{coul}(Z_{1,2}, N_{1,2}, \beta_{1,2}, d) + V_{nucl}(Z_{1,2}, N_{1,2}, \beta_{1,2}, d)$$



# The SPY model

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- A revised version of Wilkins model was developed by S. Heinrich (PhD thesis, 2006) and J.-L. Sida
- Main core of **SPY** (**S**ciSSION **P**oint model for fission fragment **Y**ields)
- Based on **microscopic ingredients**
  - Individual microscopic energies based on **HFB** calculation with the **Gogny D1S** interaction (S. Hilaire, avail. @ Amedee database)
  - No dependence on intrinsic temperature
  - **Available energy** is calculated as:

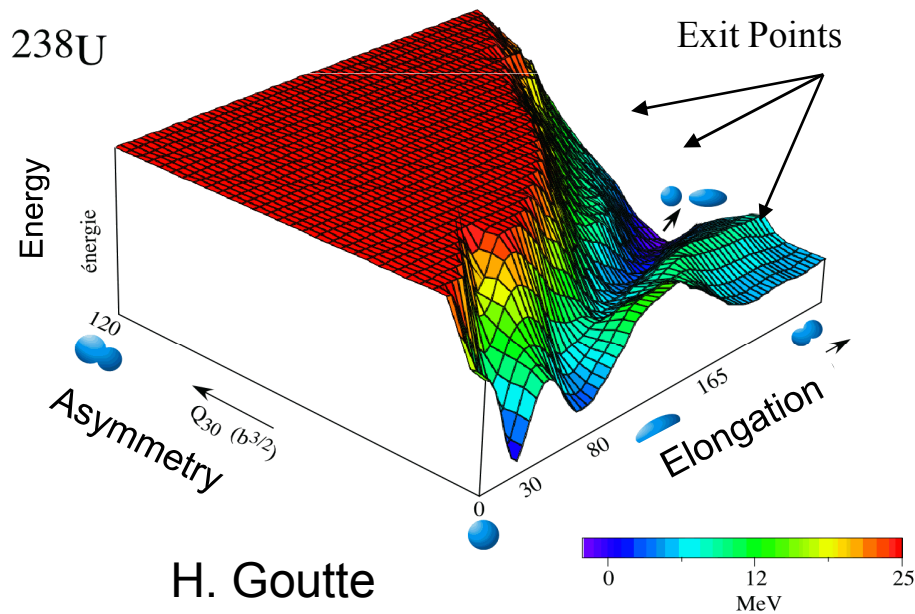
$$A = E_{\text{tot}} - V$$

$$V(Z_{1,2}, N_{1,2}, \beta_{1,2}, d) = \Sigma V_{\text{HFB}}^{1,2}(Z^{1,2}, N^{1,2}, \beta^{1,2}) \\ + V_{\text{Coul}}(Z_{1,2}, N_{1,2}, \beta_{1,2}, d) + V_{\text{nucl}}(Z_{1,2}, N_{1,2}, \beta_{1,2}, d)$$

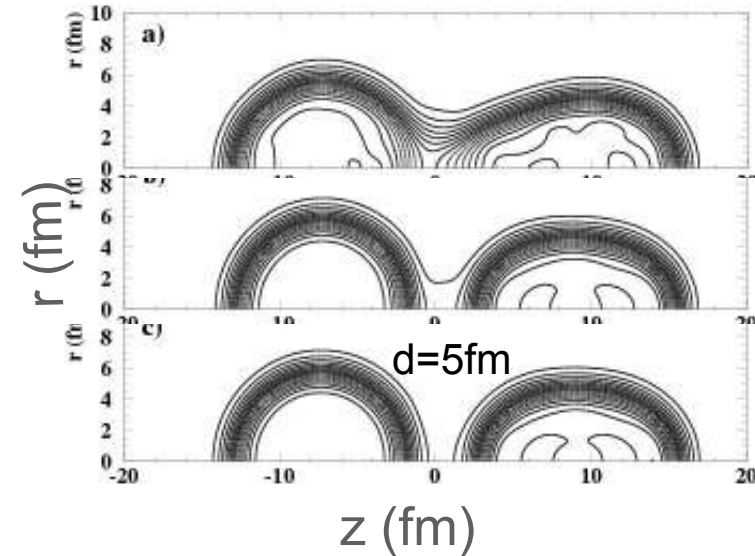
- Coulomb interaction based on Cohen Swiatecki formalism  
*Cohen and Swiatecki, Annals of Physics 19 (1962) 67*
- Nuclear interaction based on the Blocki proximity potential  
*Blocki et al, Annals of Physics 105 (1977) 427*

# On the scission point definition

- The SPY model is **parameter free**
- The distance **d** is **fixed at 5 fm**
- The distance is chosen on the exit points selection criteria used on Bruyères microscopic fission calculations



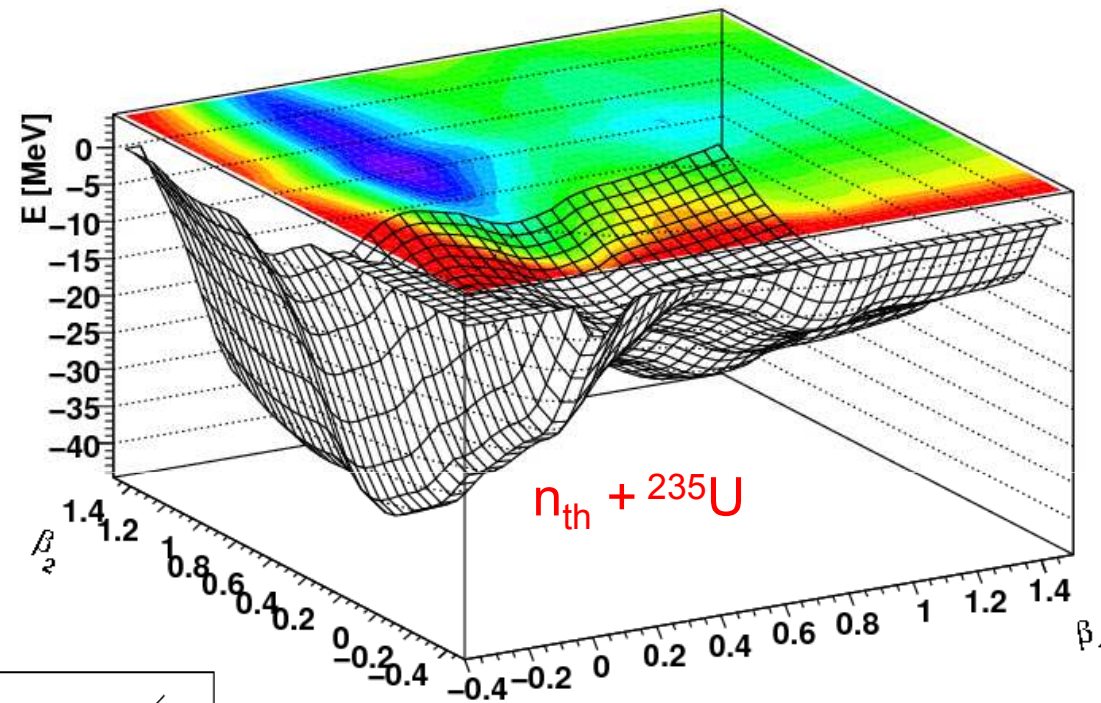
Nucleon density at the neck  $\rho < 0.01 \text{ fm}^3$   
Total binding energy drop ( $\approx 15 \text{ MeV}$ )  
Hexadecupolar moment drop ( $\approx 1/3$ )





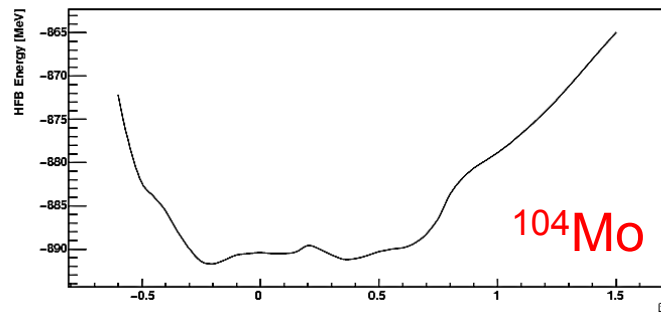
# Available energy at scission: asymmetric fragmentation

Potential Energy Surface for the fragmentation (Z=50, N=82) (Z=42, N=62)

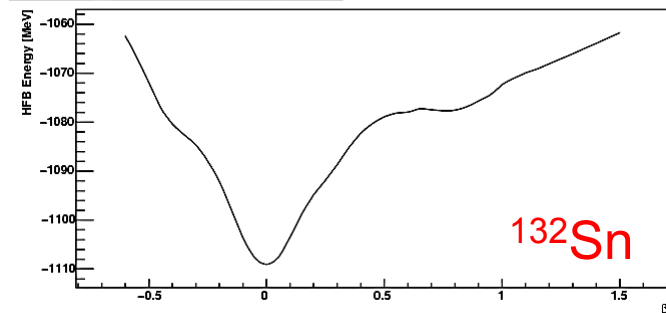


Driven by the double shell effect of spherical  $^{132}\text{Sn}$

HFB Energy of the nucleus (Z=42, N=62)



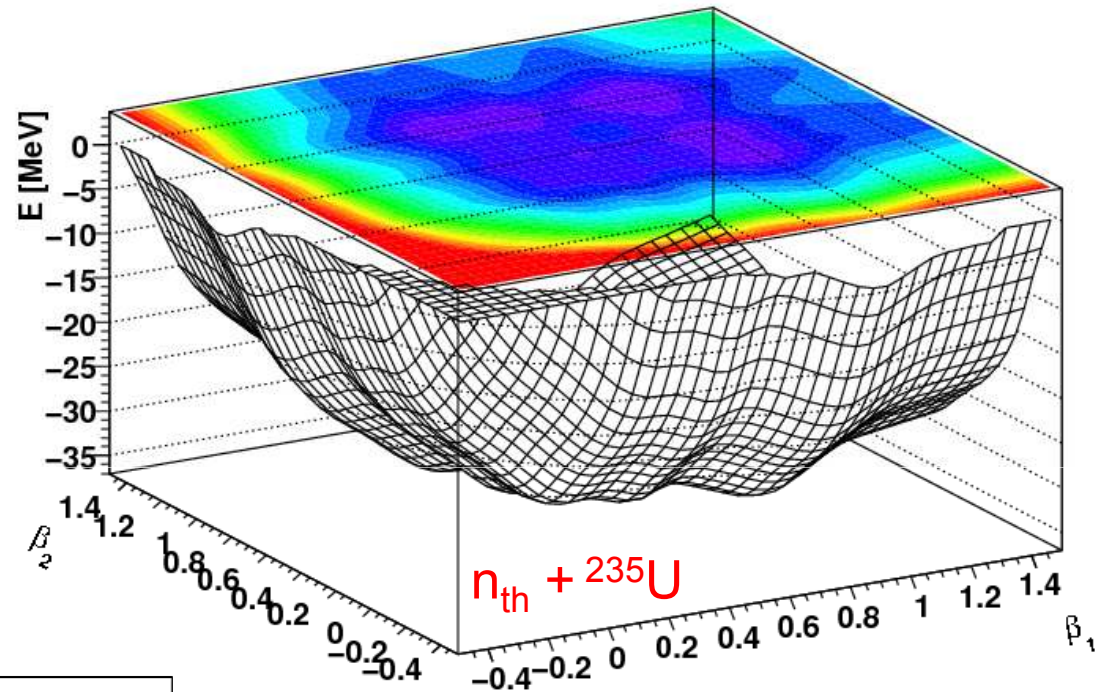
HFB Energy of the nucleus (Z=50, N=82)





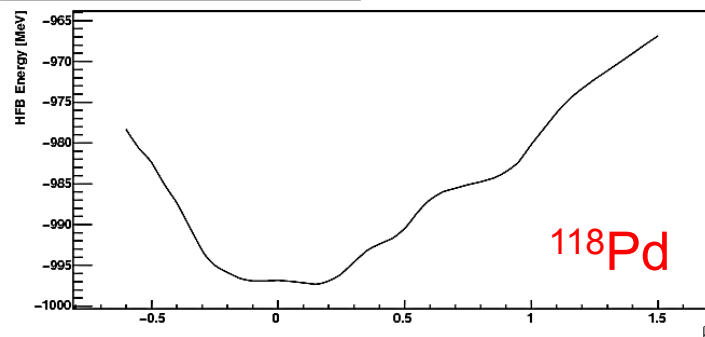
# Available energy at scission: symmetric fragmentation

Potential Energy Surface for the fragmentation ( $Z=46, N=72$ ) ( $Z=46, N=72$ )



Quite large deformations available for soft nuclei

HFB Energy of the nucleus ( $Z=46, N=72$ )



# The statistical treatment

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- The **probability of a given fragmentation** is linked to the **phase space** available at scission
- The phase space is defined by the **number of available states** of each fragment, i.e. the intrinsic **level/state density**
- The energy partition at scission is supposed to be equiprobable between each state available to the system (**microcanonical system**)
- Therefore the phase space is defined as:

$$\pi(N_l, N_h, Z_l, Z_h, \beta_l, \beta_h, A) = \int_{\varepsilon=0}^{\varepsilon=A} \rho_l(\beta_l, \varepsilon) \rho_h(\beta_h, A - \varepsilon) d\varepsilon$$

- The relative probability of a given fragment pair is:

$$P(N_l, N_h, Z_l, Z_h) = \int_0^{\beta_{\max}} \int_0^{\beta_{\max}} \pi(\dots, \beta_l, \beta_h, A) d\beta_l d\beta_h$$

# The level density ingredient

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- Very delicate point of the model...
- In this approach the level densities are a **natural counterbalance** to a stronger stabilization of spherical deformations and even-even nuclei, which leads to unphysical fragment mass distributions
- For the time being, a **Fermi gas approach** has been tested
- The **CTM effective** level density is parameterized as:

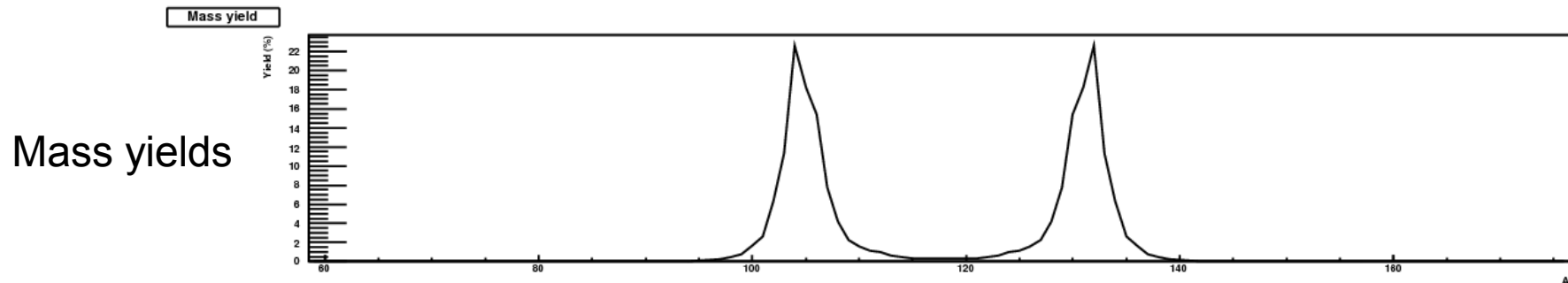
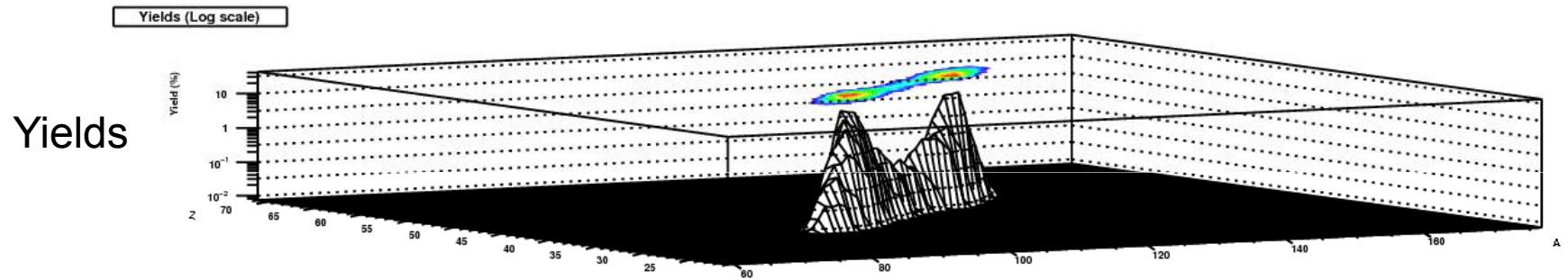
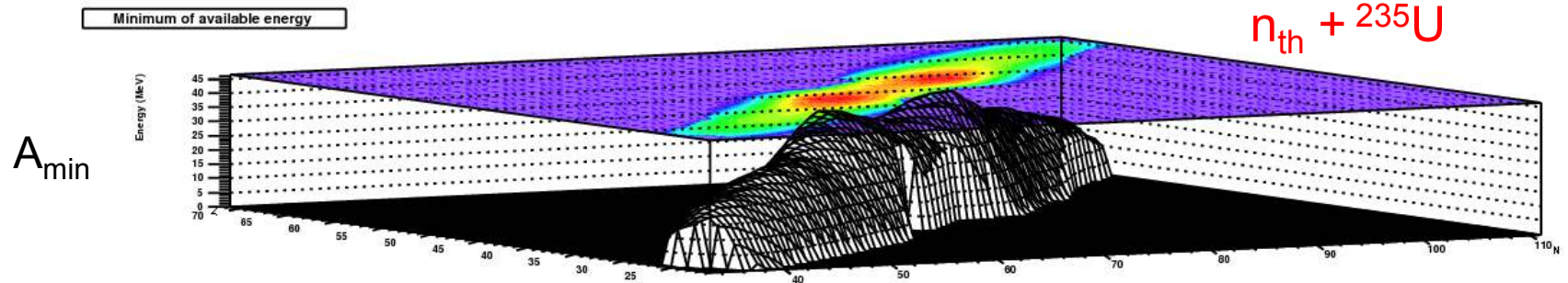
*Koning et al., Nucl. Phys. A 810 (2008) 13*

$$\rho_F(E) = \frac{1}{\sqrt{2\pi}\sigma} \frac{\sqrt{\pi}}{12} \frac{e^{2\sqrt{aE}}}{a^{1/4} E^{5/4}}$$

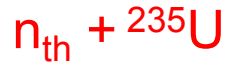
with  $a = \alpha A + \beta A^{2/3}$ ,  $\alpha = 0.0692559$ ,  $\beta = 0.282769$   
and  $\sigma = I_0 a \sqrt{E} / a$

- A **microscopic calculation** of level densities is actually performed (at zero temperature) in the framework of HFB formalism by S. Hilaire
- Very time consuming since we need the energy evolution at each deformation for some hundreds of nuclei

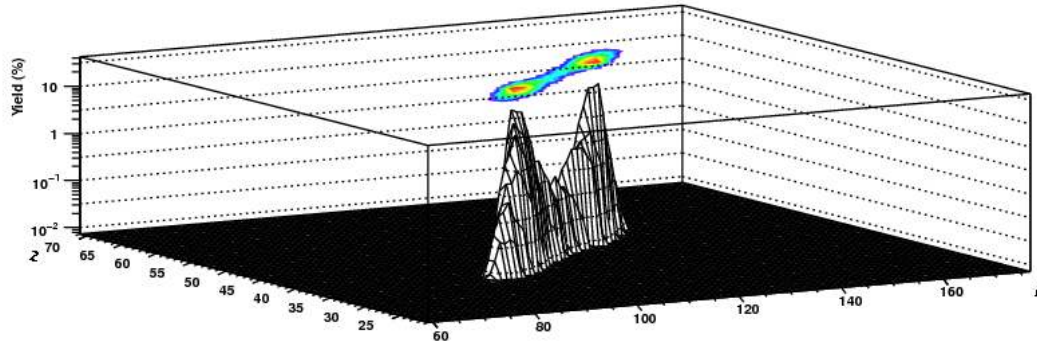
# From the available energy to the yield



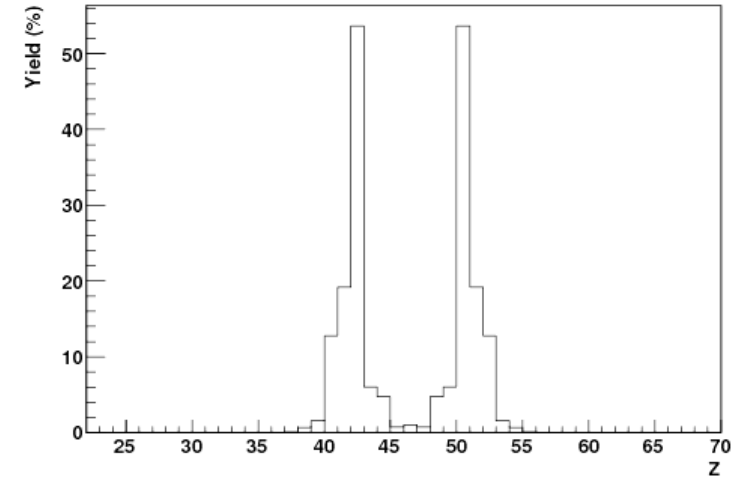
# Observables: mass and charge yields



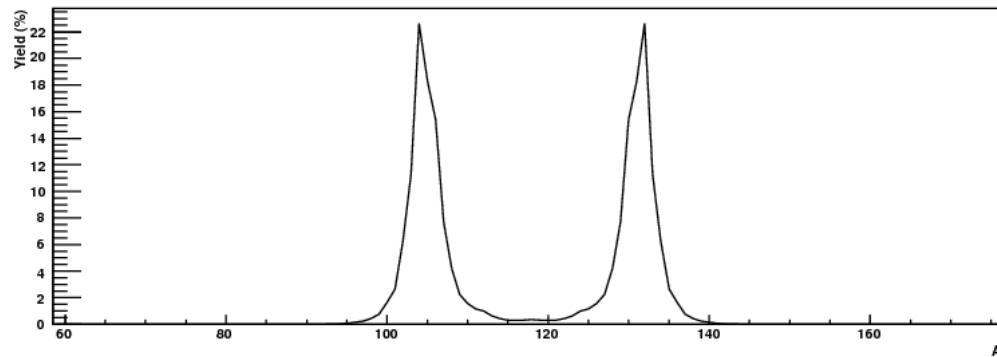
Yields (Log scale)



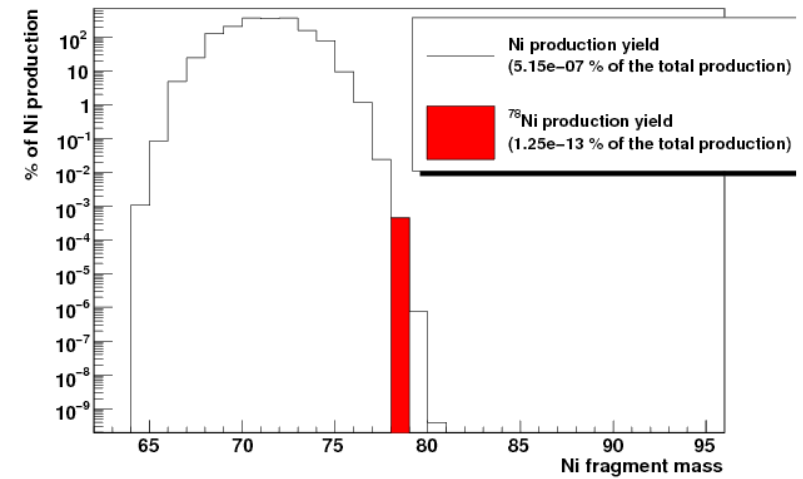
Z yield



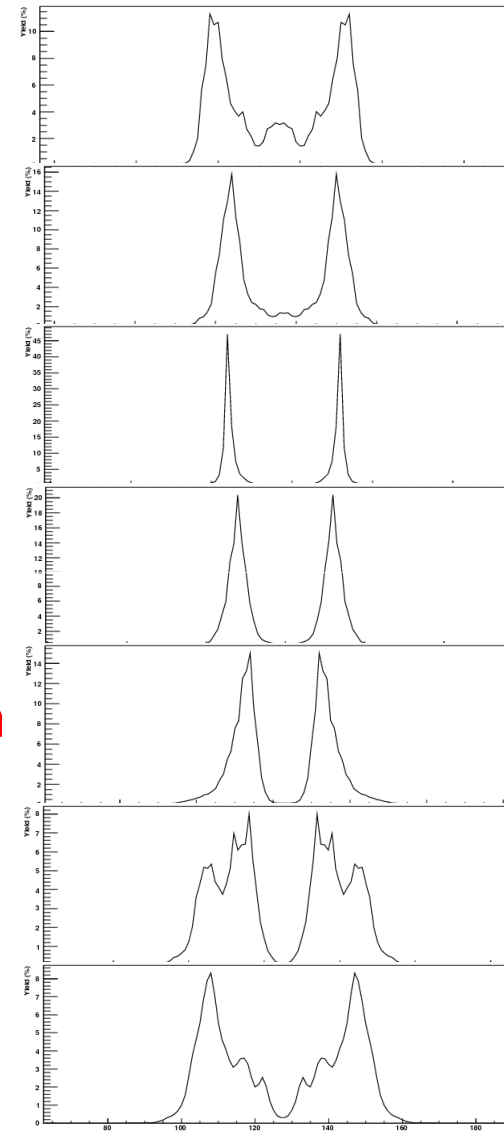
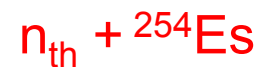
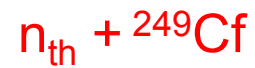
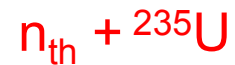
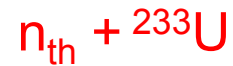
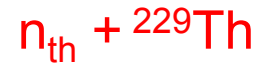
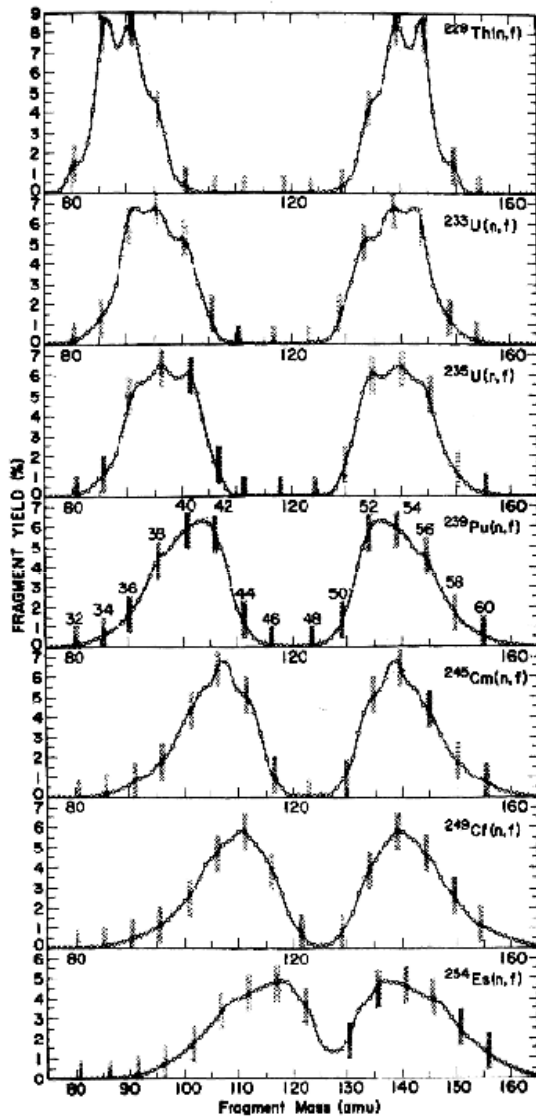
Mass yield



Ni production yield for  ${}^{235}\text{U}$  thermal fission

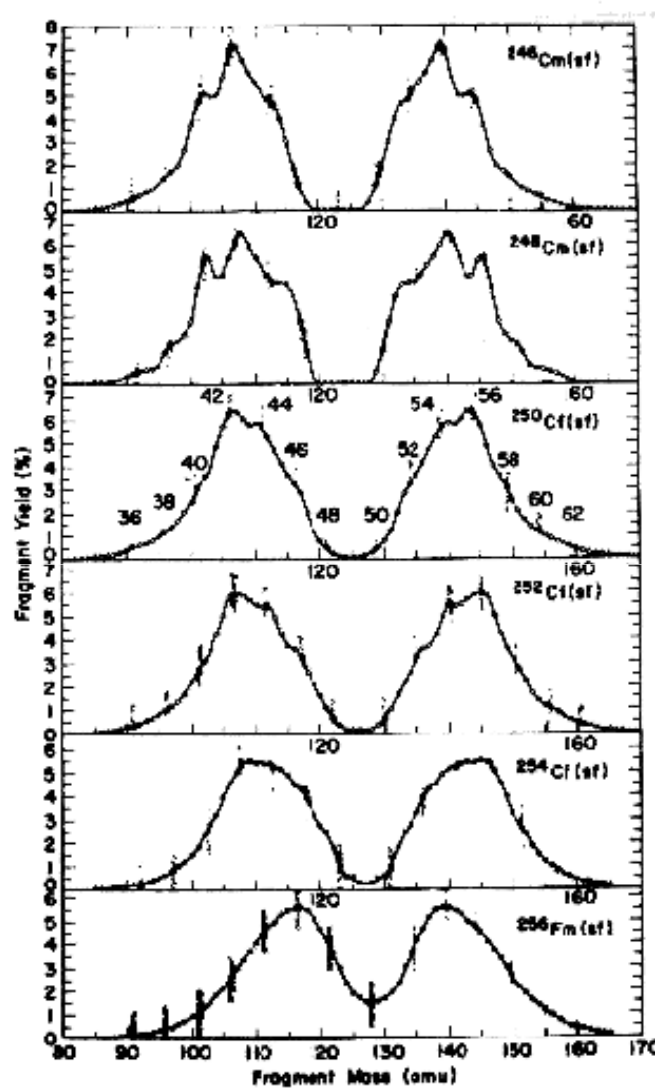


# Systematics: mass yields for n-induced fission





# Systematics: mass yields for spontaneous fission



246Cm(sf)

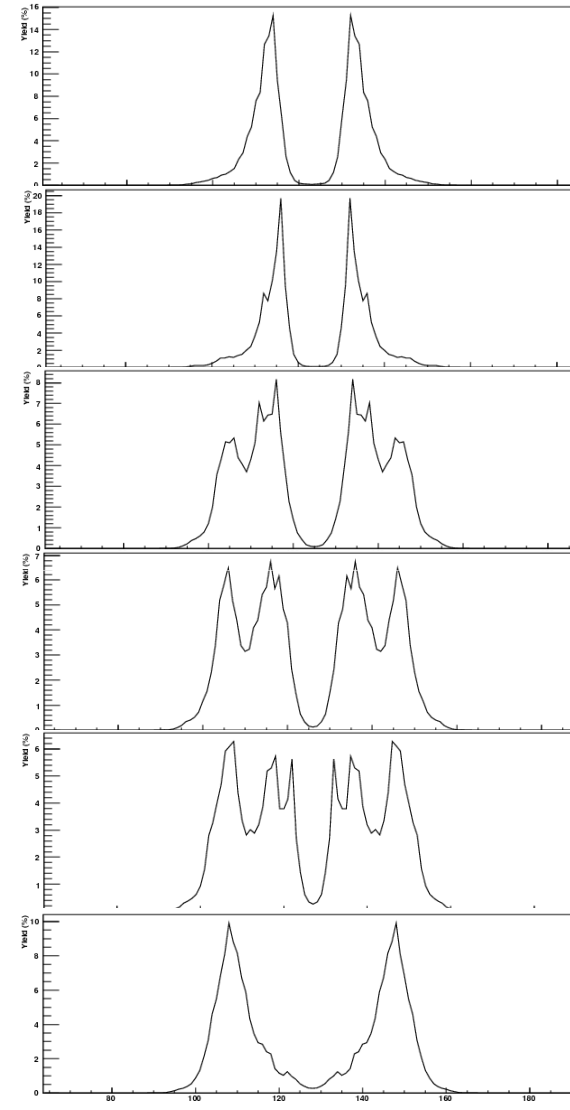
248Cm(sf)

250Cf(sf)

252Cf(sf)

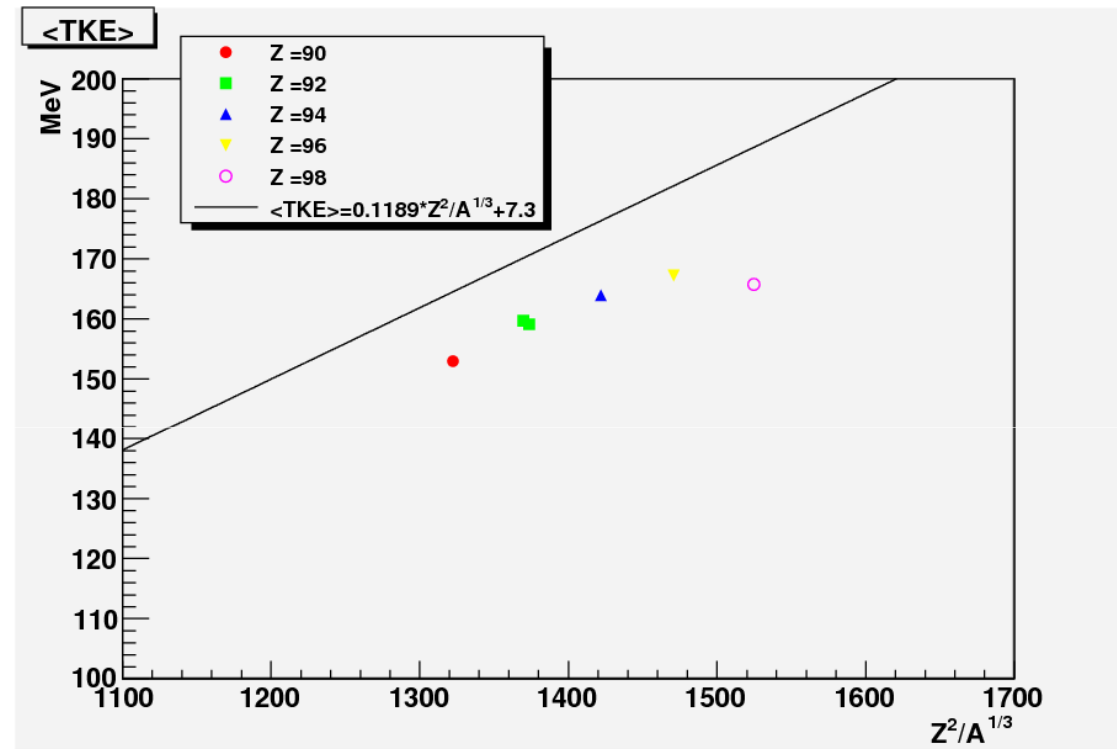
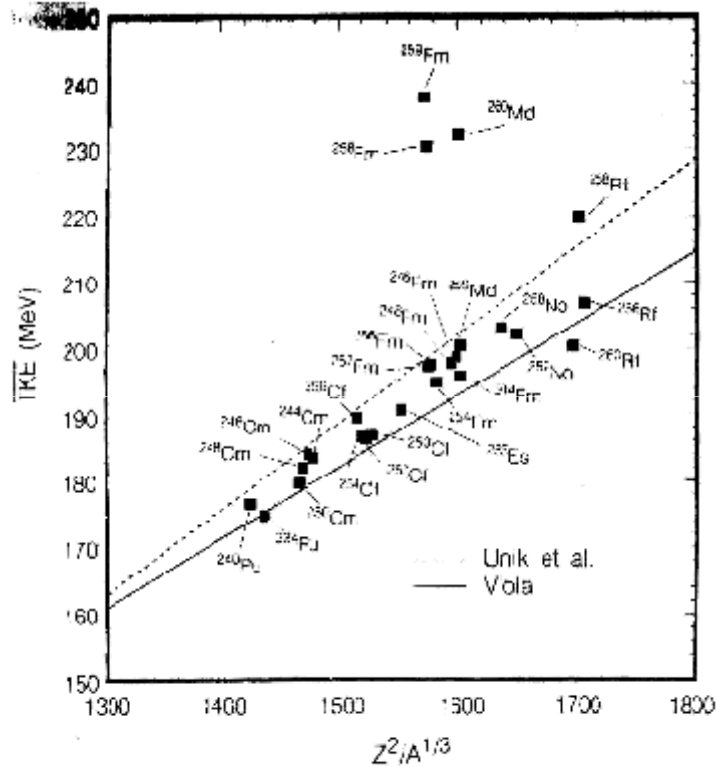
254Cf(sf)

256Fm(sf)



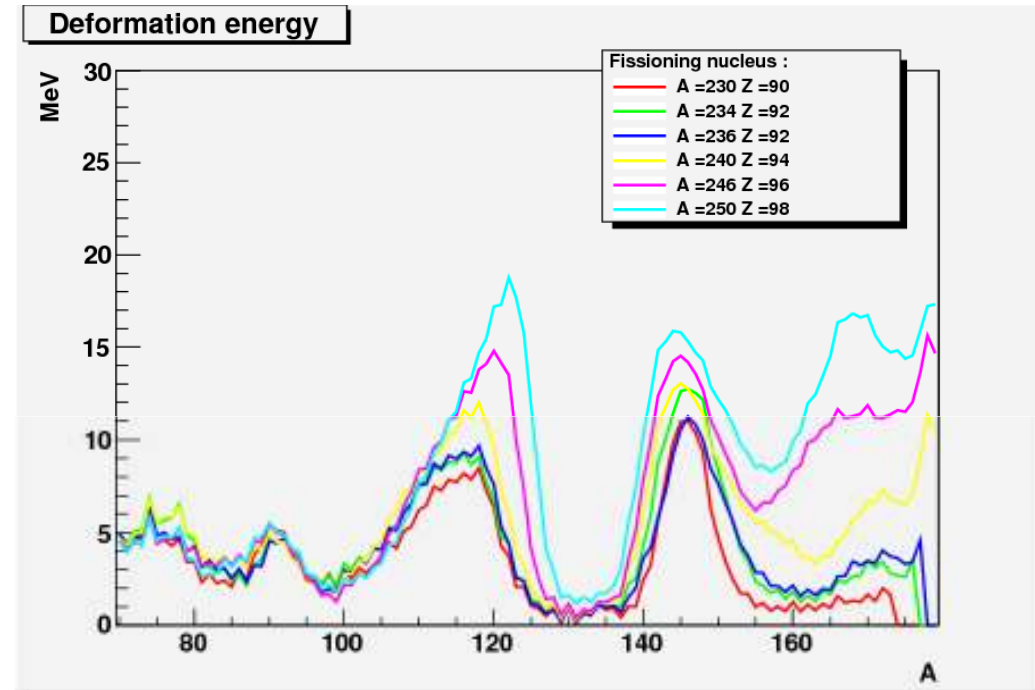
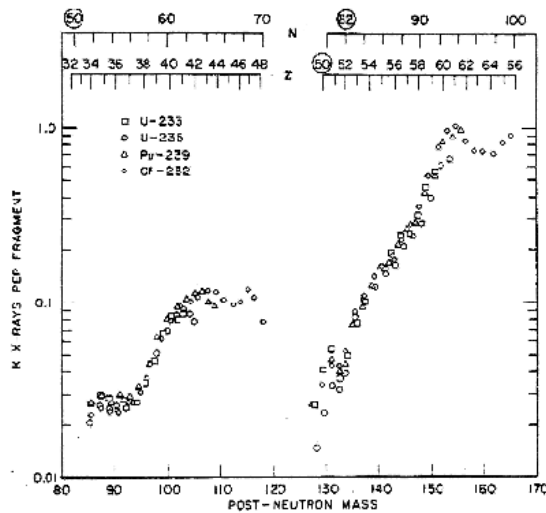
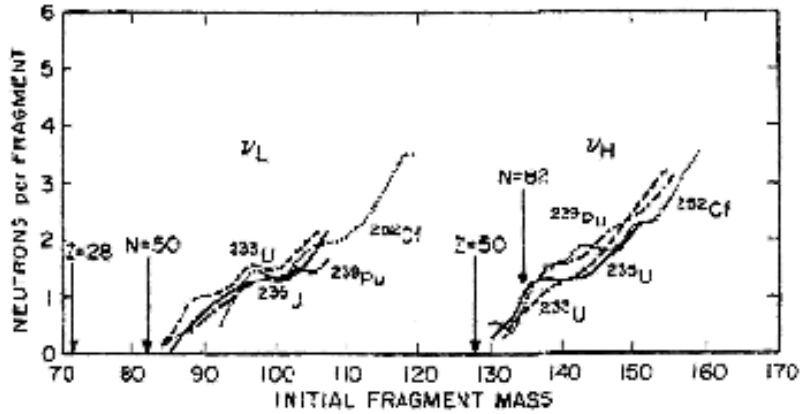


# Systematics: mean TKE



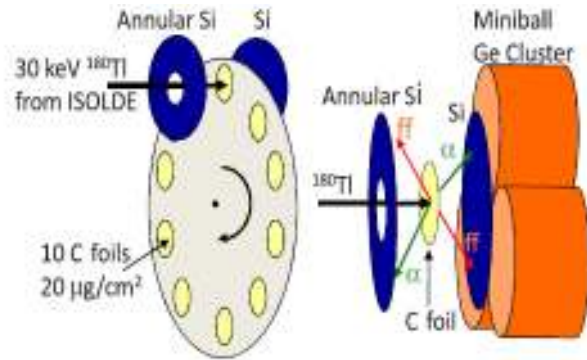
We miss around 10 MeV: pre-scission energy (d dependence), Coulomb?

# Systematics: mean deformation energy

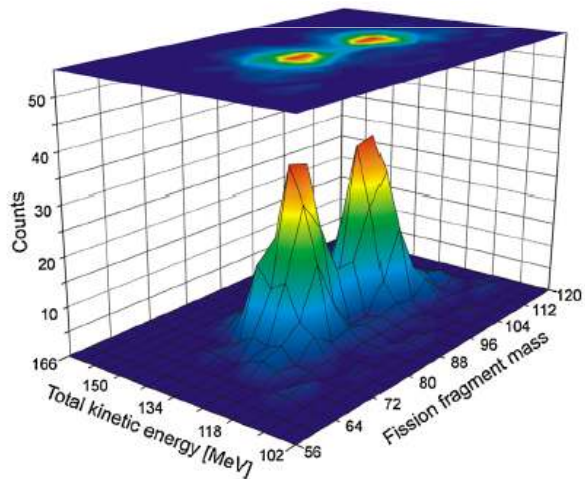


The deformation energy is somehow related to the number of emitted particles

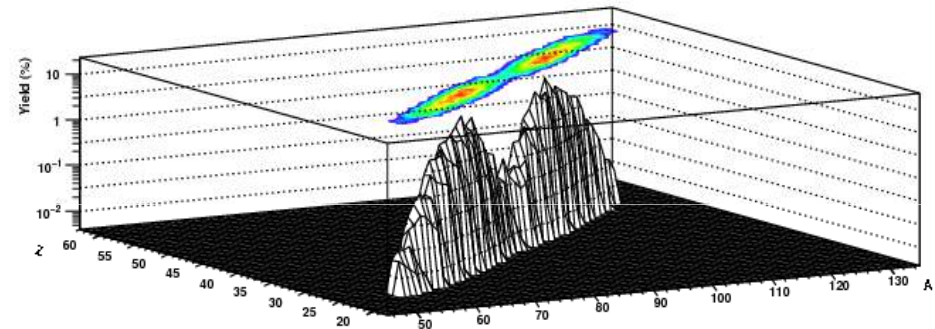
# SPY can already participate to a hot debate...



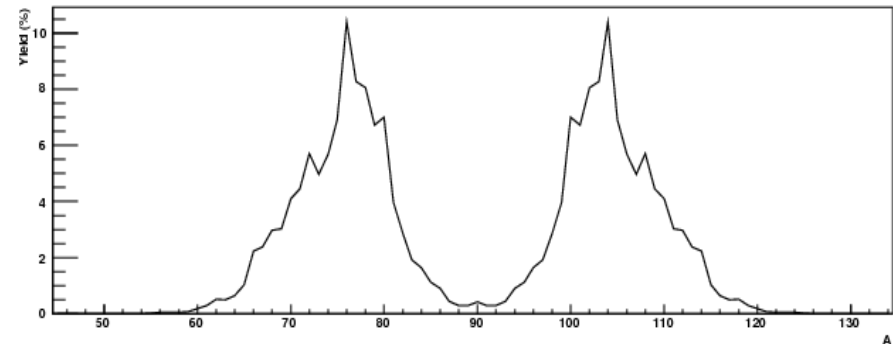
$\beta$ -delayed fission of  $^{180}\text{Tl}$   
 Surprising **asymmetric yields of  $^{180}\text{Hg}$  fission** fully attributed to the nuclear structure of the fissioning nucleus



Yields (Log scale)



Mass yield



Andreyev et al., PRL 105 (2010) 252502

# Conclusions and perspectives

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- We are developing a statistical scission-point model fully based on microscopic ingredients
- Work in progress but first **results are encouraging**
- The **lack of dynamics** is visible (width of yields distributions)
- More work needed on:
  - Coulomb interaction calculation
  - Take into account **pre-scission energy** into the balance (this can wash out the dependence on  $d$ )
  - **Level density calculations (for “quasi” beginners...)**
    - What is the best parametrization?
    - How to parameterize the beta dependence?
    - Is the  $E$  dependence really smooth (like Fermi gas)?
    - Microscopic level densities are a useless effort (besides the coherence of the microscopic approach)?
    - Is the spin/parity dependence well under control?
  - Integration of HFB calculation at finite temperature ( $E^* \approx T^2$ )
  - Integration of full spin populations to calculate isomeric yields
  - ...