

The two-step (and multiple-step) γ cascade method as a tool for studying γ -ray strength functions

Milan Krtička

CHARLES UNIVERSITY PRAGUE

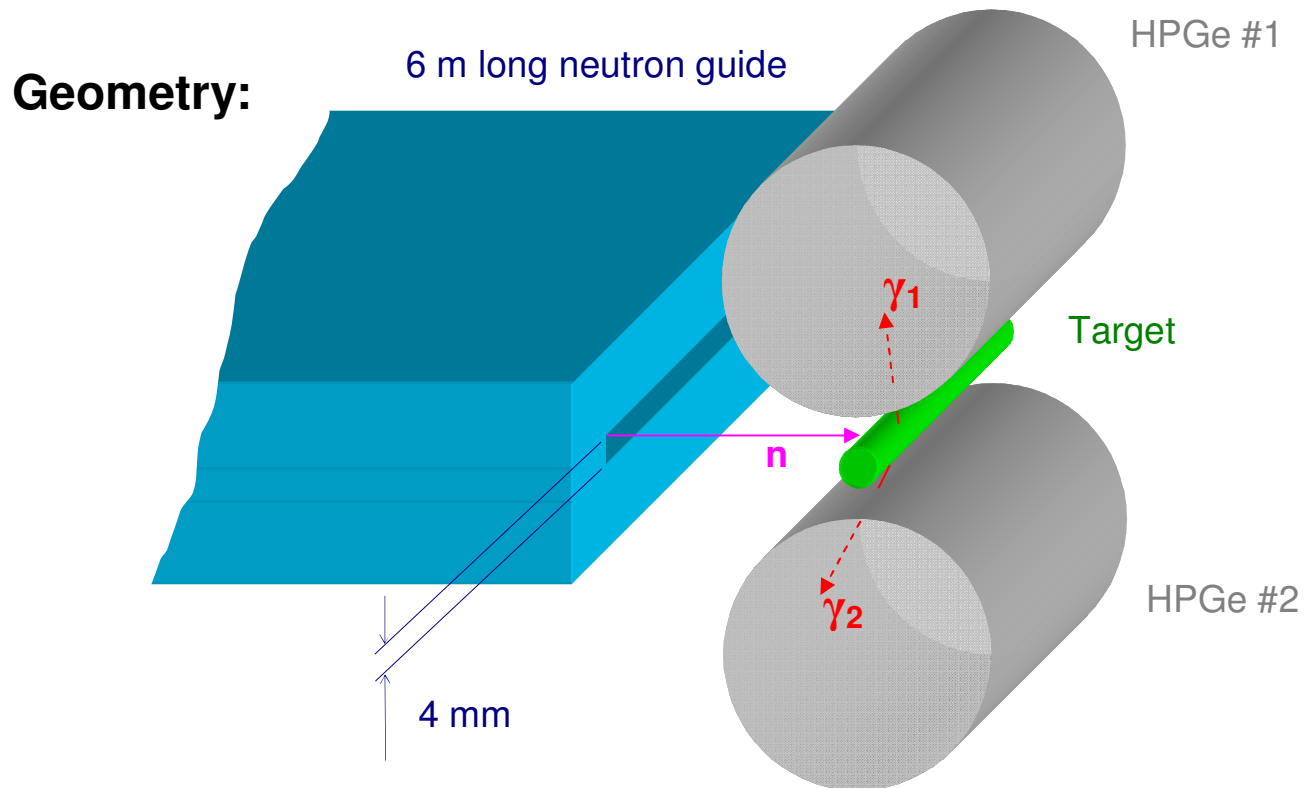
faculty of mathematics and physics



Outline

- The method of two-step γ -cascades following thermal neutron capture
(setup at Rez near Prague)
- Two-step (multi-step) γ -cascades following resonance neutron capture
(DANCE - LANL)
- Data processing - DICEBOX code
- Examples / Results
(Enhancement of PSFs at low energies, Scissors mode)

The method of two-step γ -cascades following TNC



Data acquisition:

Three-parametric, list-mode

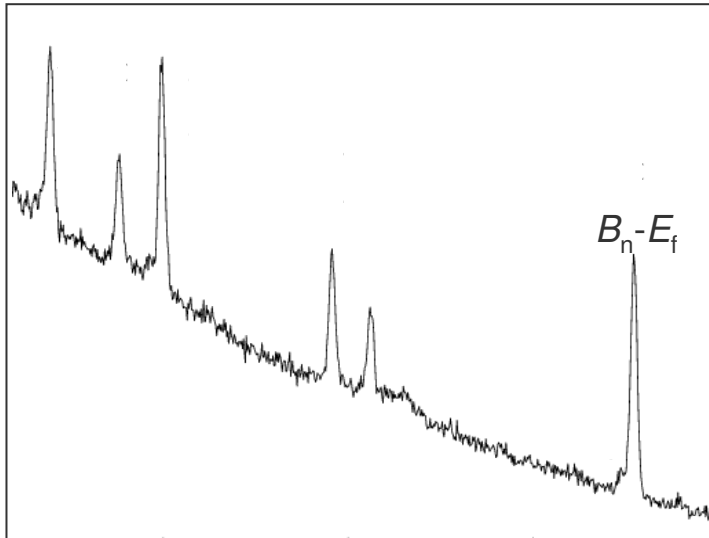
- Energy E_{γ_1}
- Energy E_{γ_2}
- Detection-time difference



Oslo, May 11, 2009

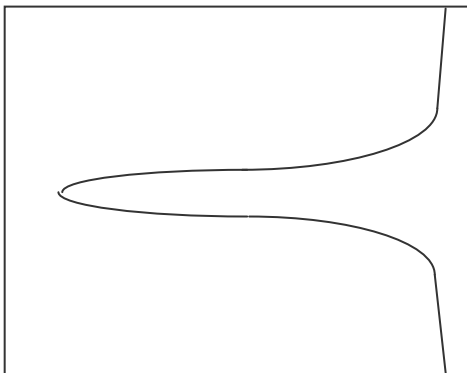
TSC spectra

Spectrum of energy sums

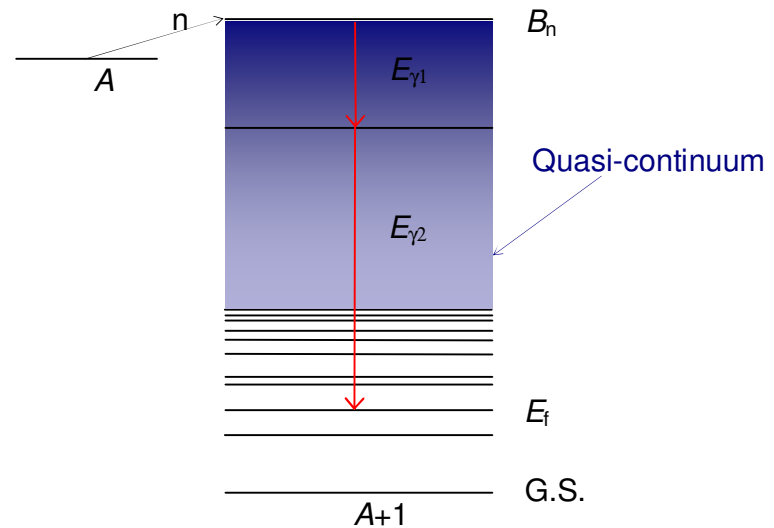
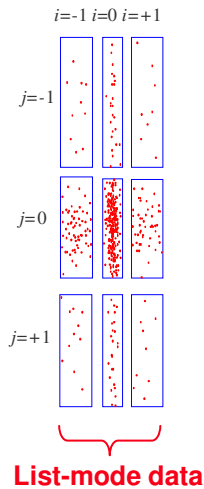


Energy sum $E_{\gamma 1} + E_{\gamma 2}$

Time response function



Detection-time difference



Accumulation of the TSC spectrum from, say, detector #1:

The contents of the bin, belonging to the energy $E_{\gamma 1}$, is incremented by

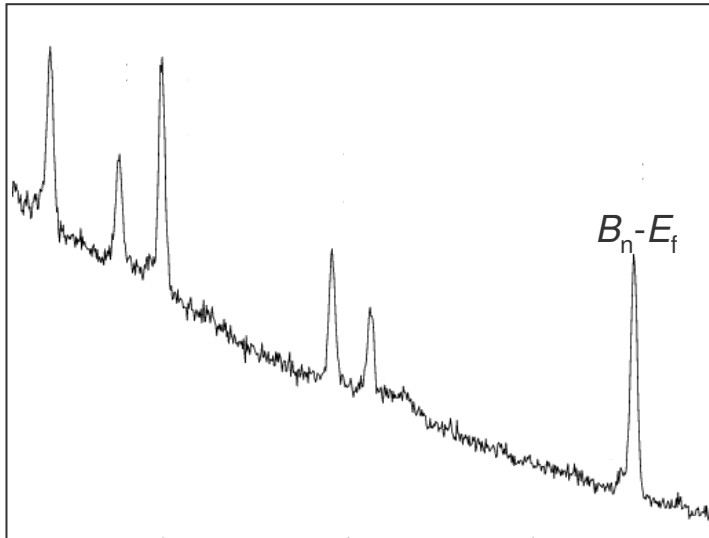
$$q = \alpha_{ij}$$

where α_{ij} is given by the position and the size of the corresponding window in the 2D space “detection time” \times “energy sum $E_{\gamma 1} + E_{\gamma 2}$ ”.

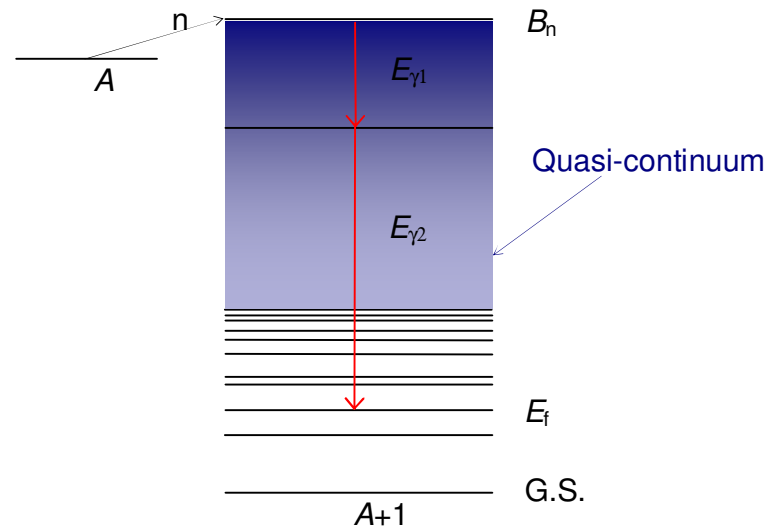
\Rightarrow background-free spectrum

TSC spectra

Spectrum of energy sums

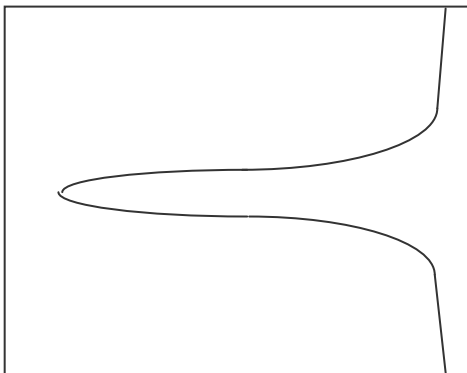


Energy sum $E_{\gamma 1} + E_{\gamma 2}$

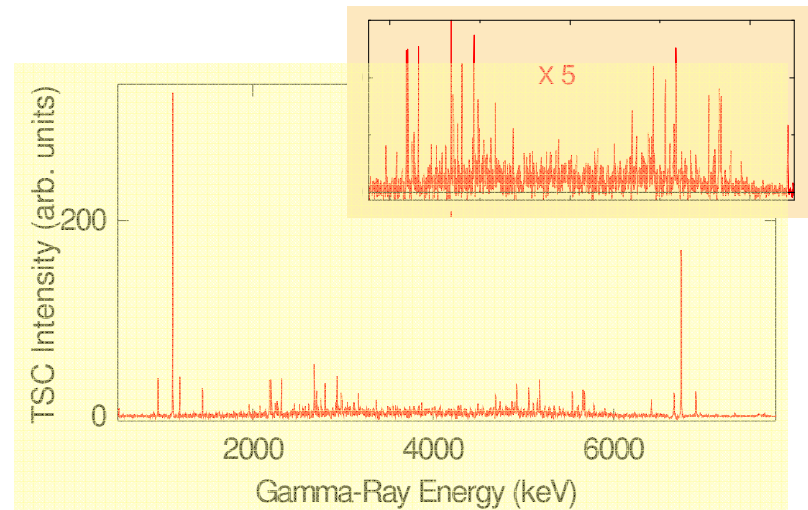
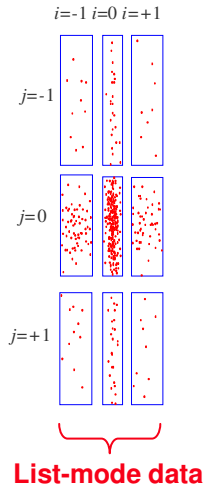


TSC spectrum - taken from **only one** of the detectors

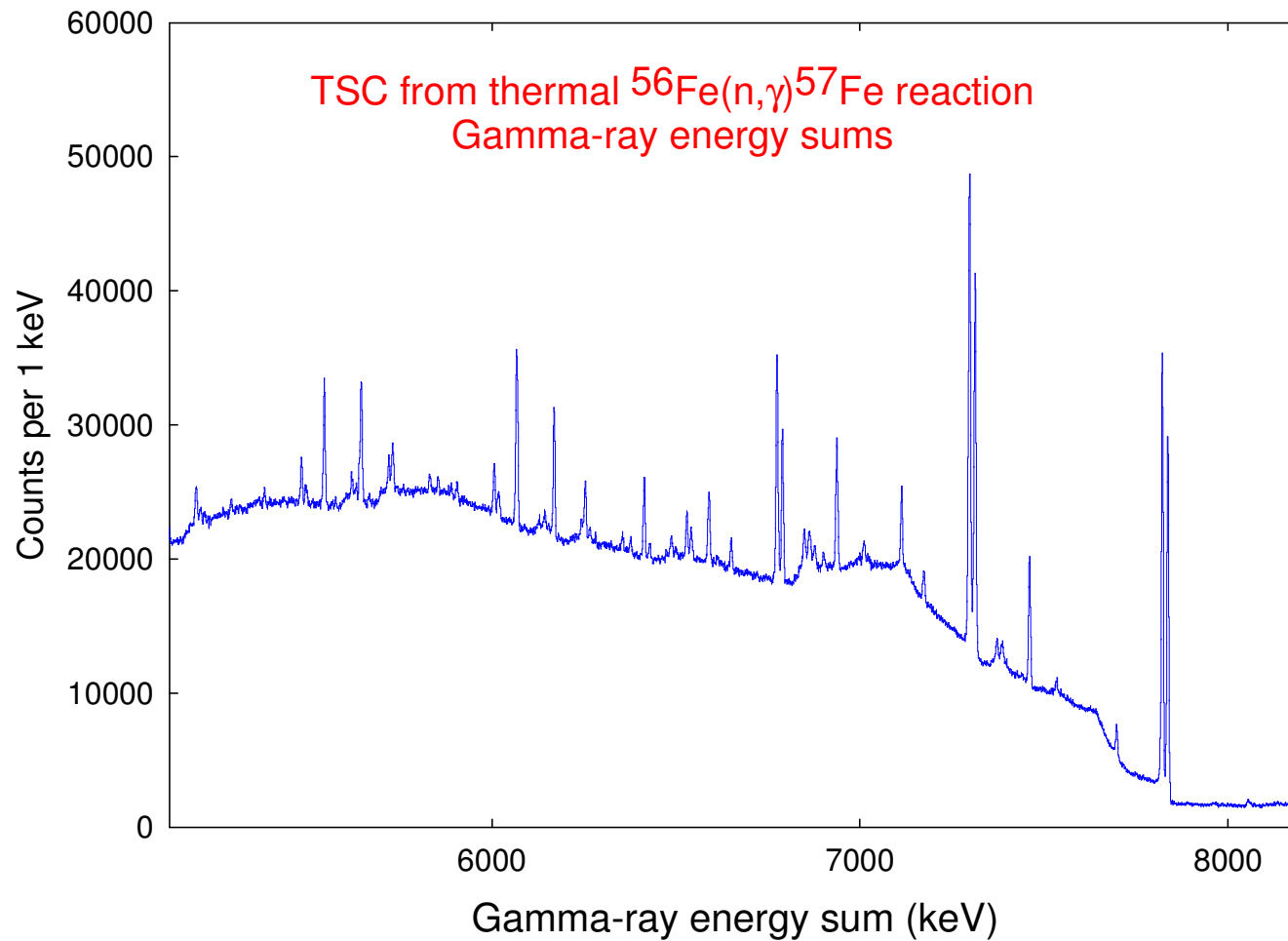
Time response function



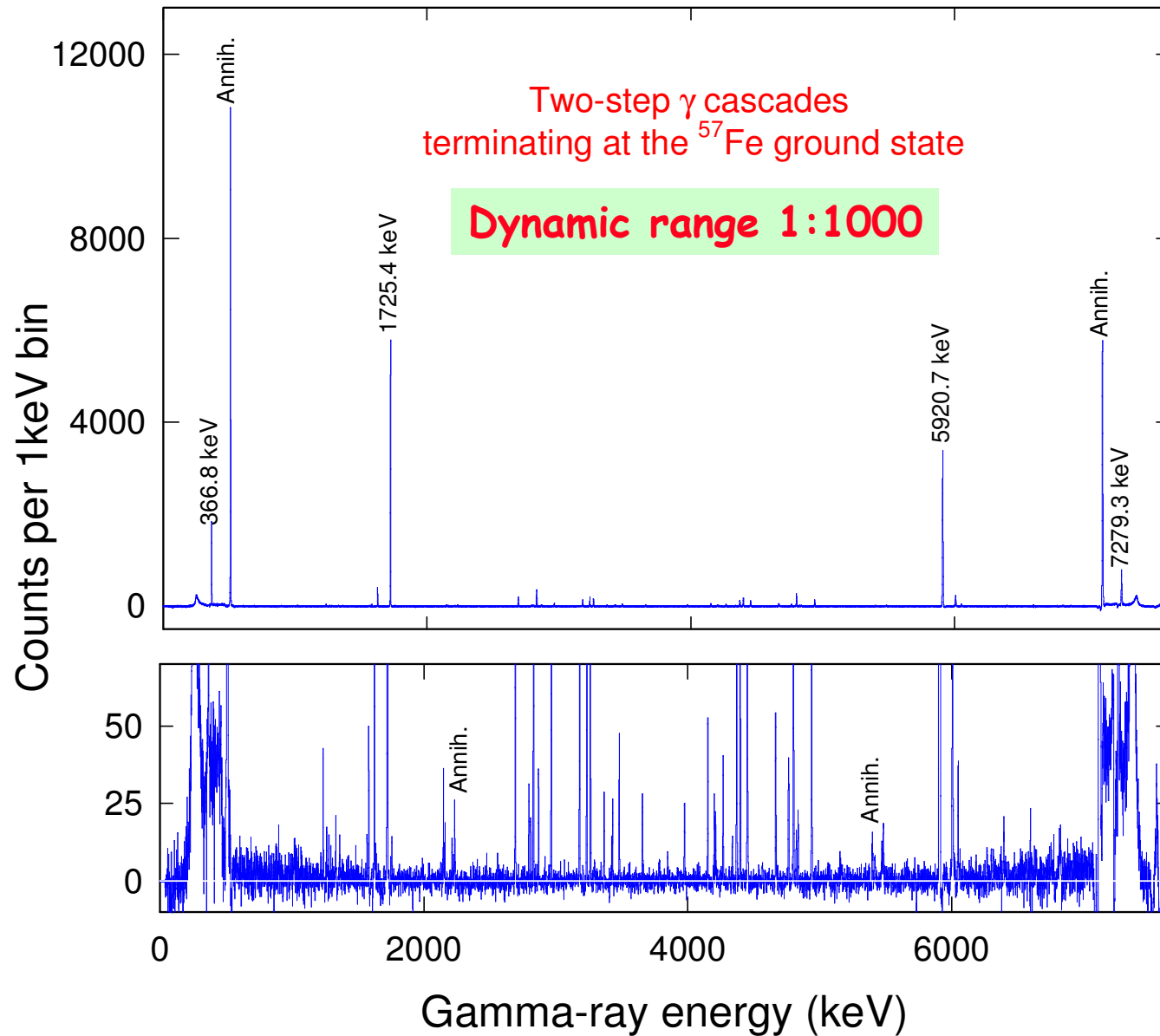
Detection-time difference



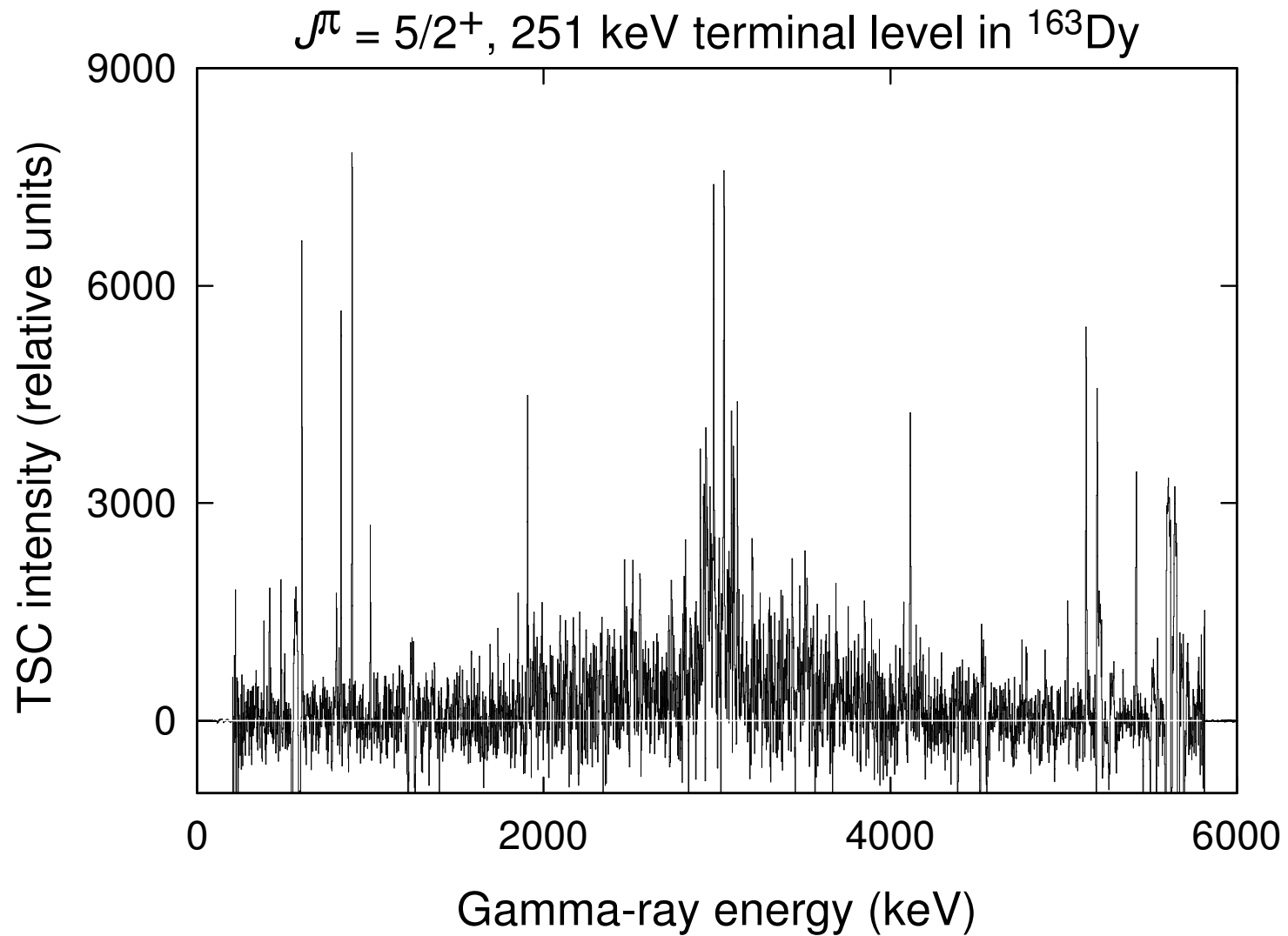
Example of sum-energy spectra (^{57}Fe)



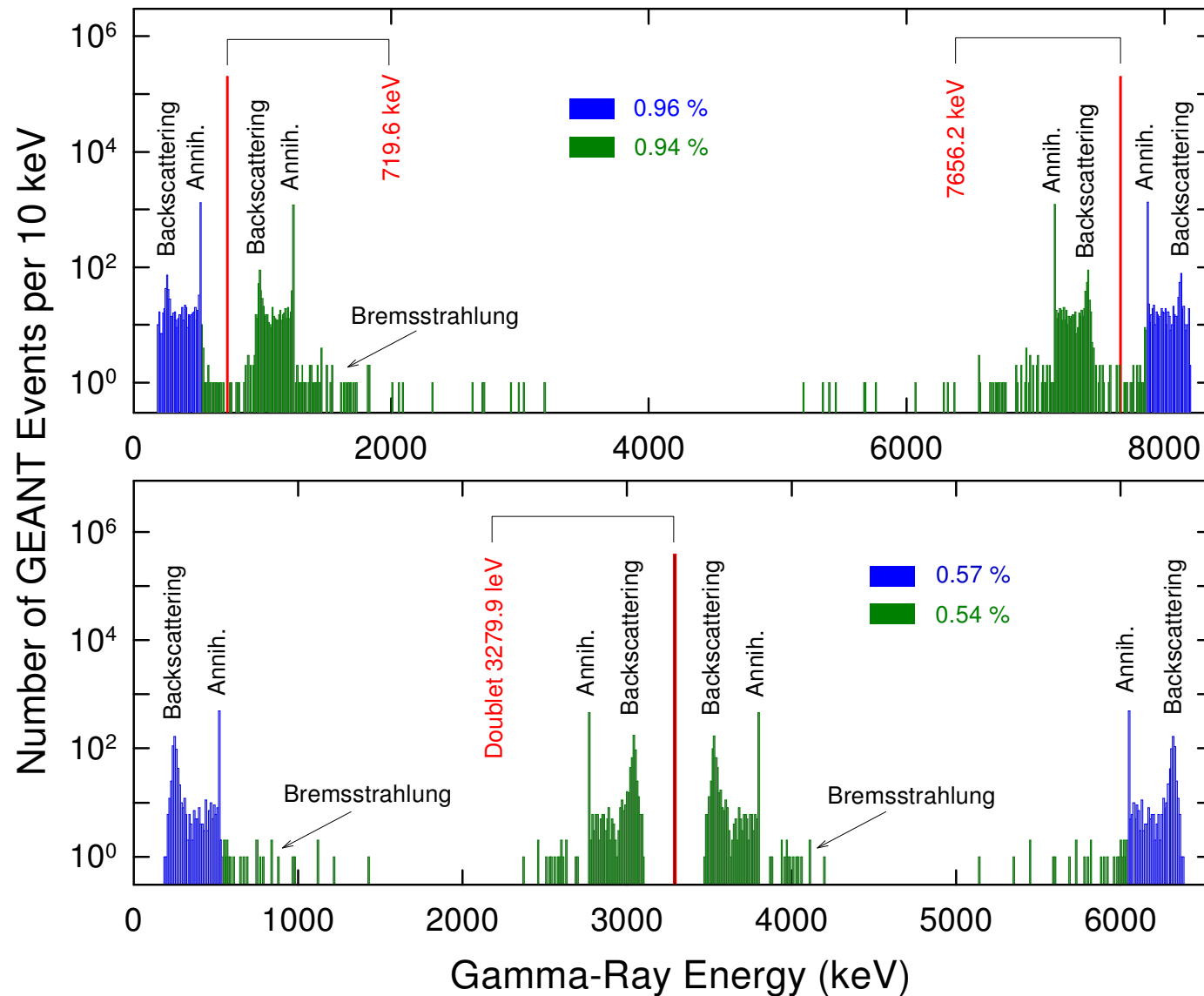
Example of a TSC spectrum



Example of a TSC spectrum



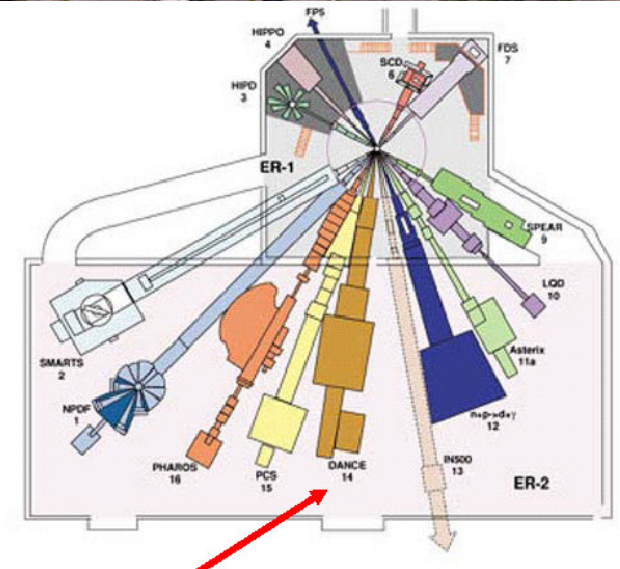
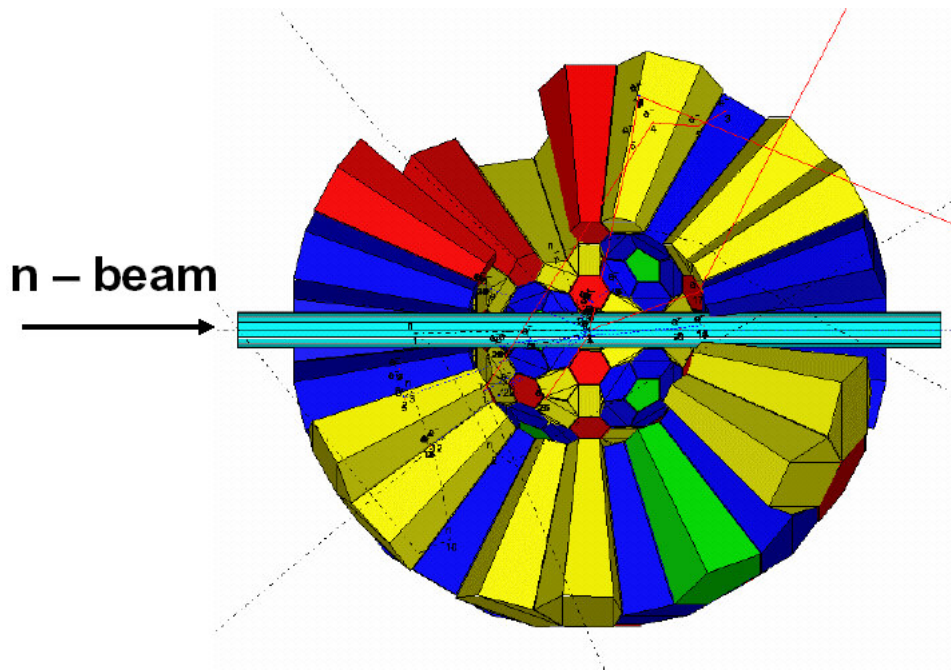
Results of GEANT3 simulations - $^{95}\text{Mo}(n,\gamma)^{96}\text{Mo}$



-
- Two-step (multi-step) γ -cascades following neutron capture with higher energies (in the region of resolved or unresolved resonances)
 - Measured with BaF₂ detector array (DANCE – LANL, n_TOF)

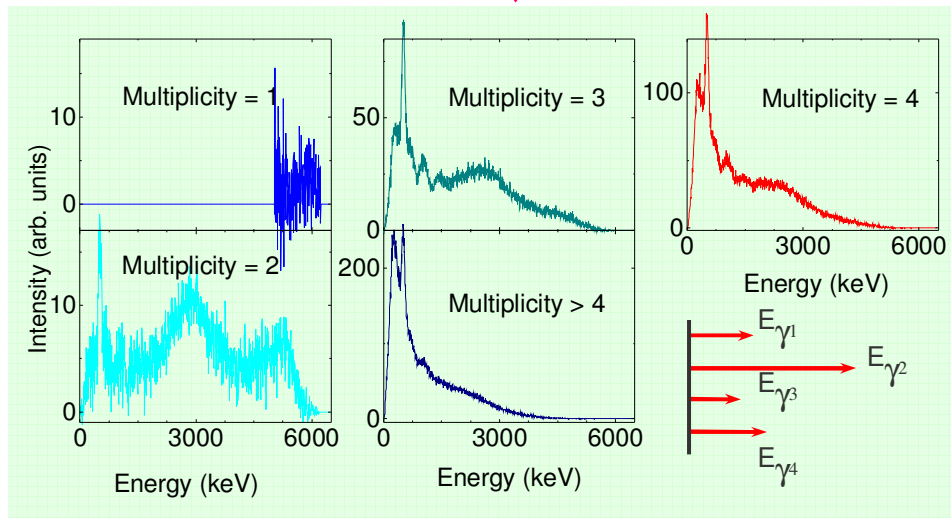
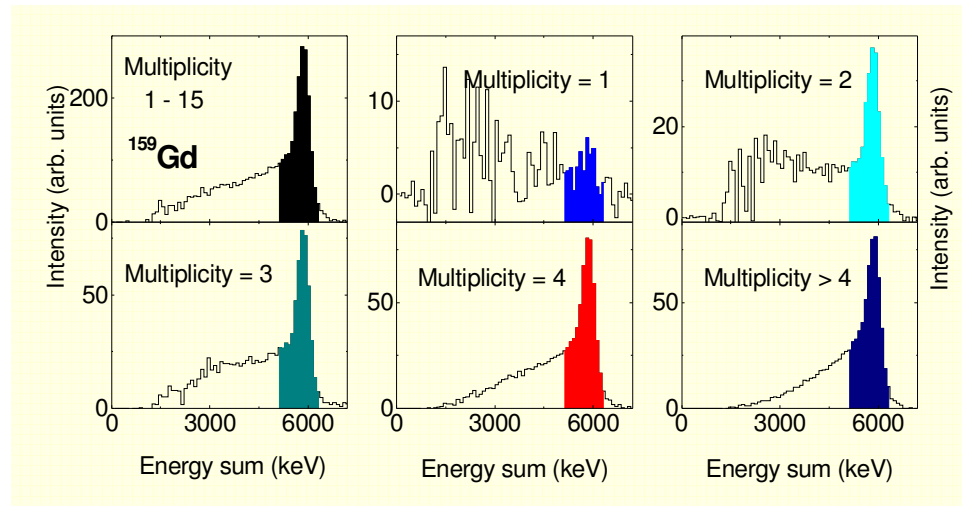
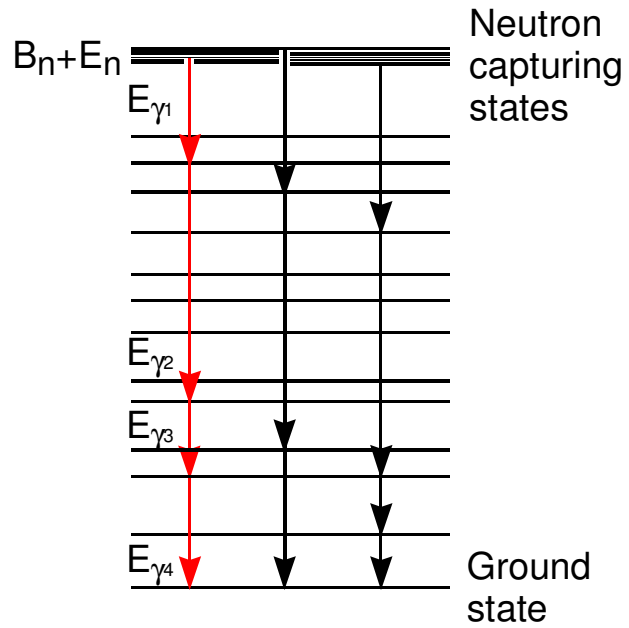
DANCE @ LANSCE

- Moderated W target gives “white” neutron spectrum, ~ 14 n’s/proton
- DANCE is on a 20 m flight path / ~ 1 cm @ beam after collimation
- repetition rate 20 Hz
- pulse width ≈ 125 ns
- DANCE consists of 160 BaF₂ crystals

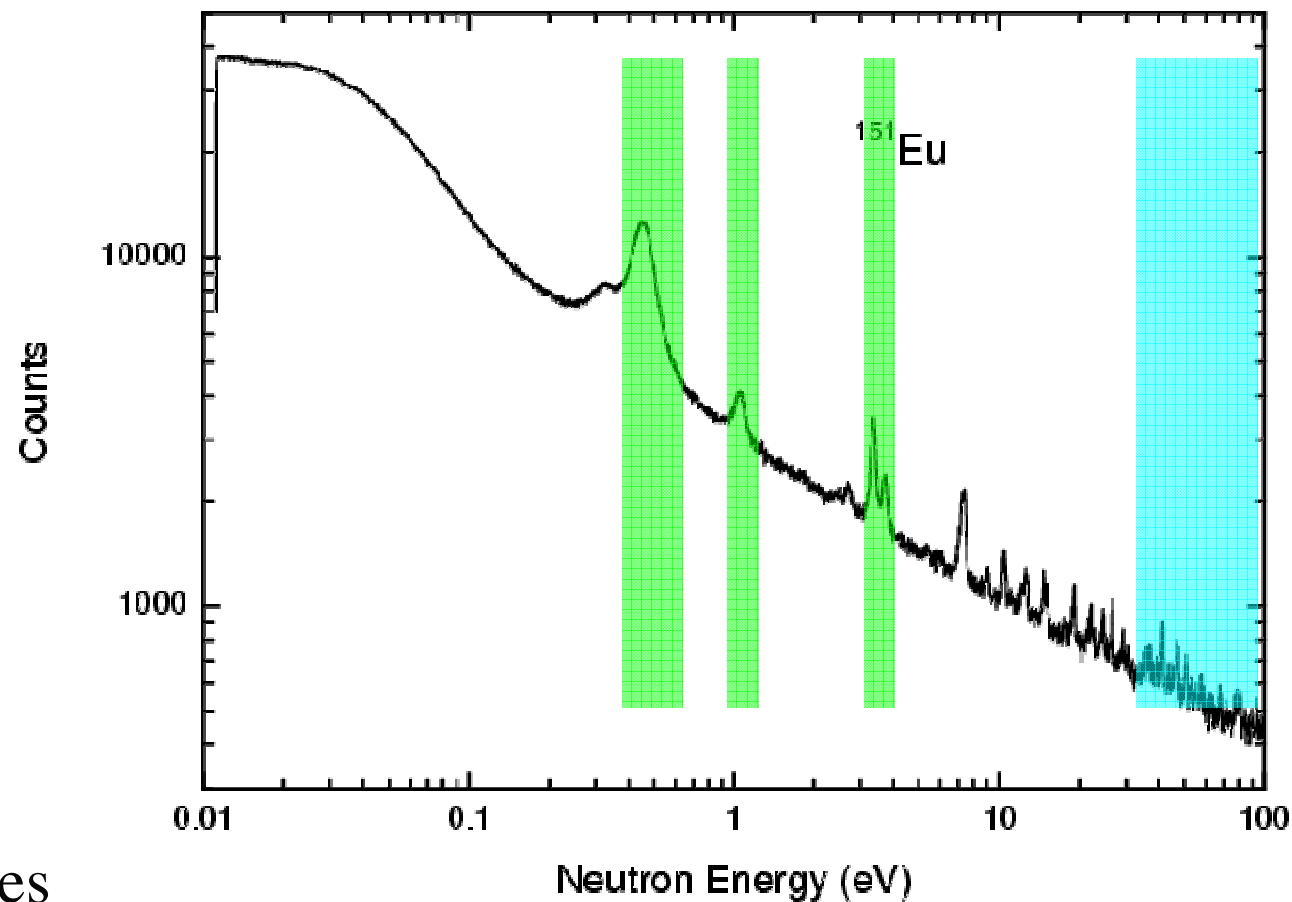


Oslo, May 11, 2009

What can be checked?



What can be checked?

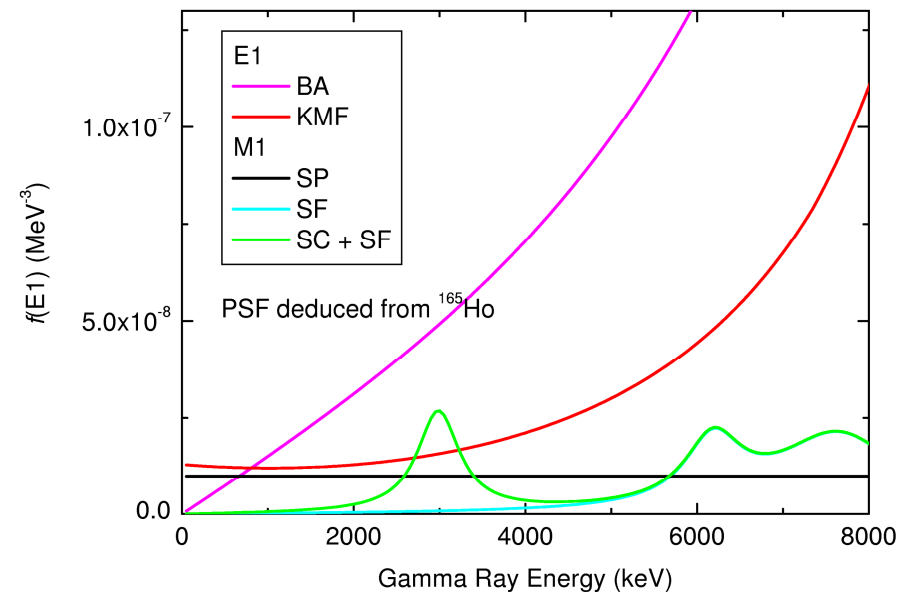
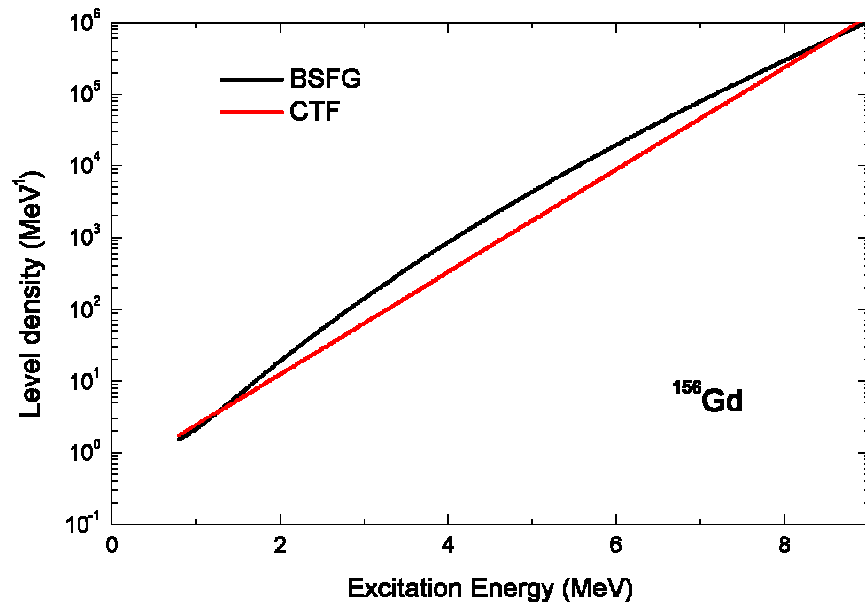


We can gate on

- strong resonances
(spectra from different resonance spins
can be compared)
- unresolved region

How to process data from these experiments?

- Result of interplay of level density and γ -ray SF



- Comparison with predictions from decay governed by different level density formulas and γ -ray strength functions
- Code DICEBOX is used for making these simulations
 - ◆ Simulates gamma decay of a compound nucleus within extreme statistical model

Simulation of γ cascades - DICEBOX algorithm

Main assumptions:

- For nuclear levels below certain “critical energy” spin, parity and decay properties are known from experiments
- Energies, spins and parities of the remaining levels are assumed to be a random discretization of an *a priori* known level-density formula
- A partial radiation width $\Gamma_{if}^{(XL)}$, characterizing a decay of a level i to a level f , is a random realization of a chi-square-distributed quantity the expectation value of which is equal to

$$f^{(XL)}(E_\gamma) E_\gamma^{2L+1} / \rho(E_i),$$

where $f^{(XL)}$ and ρ are also *a priori* known

- Selection rules governing the γ decay are taken into account
- Any pair of partial radiation widths $\Gamma_{if}^{(XL)}$ is statistically uncorrelated

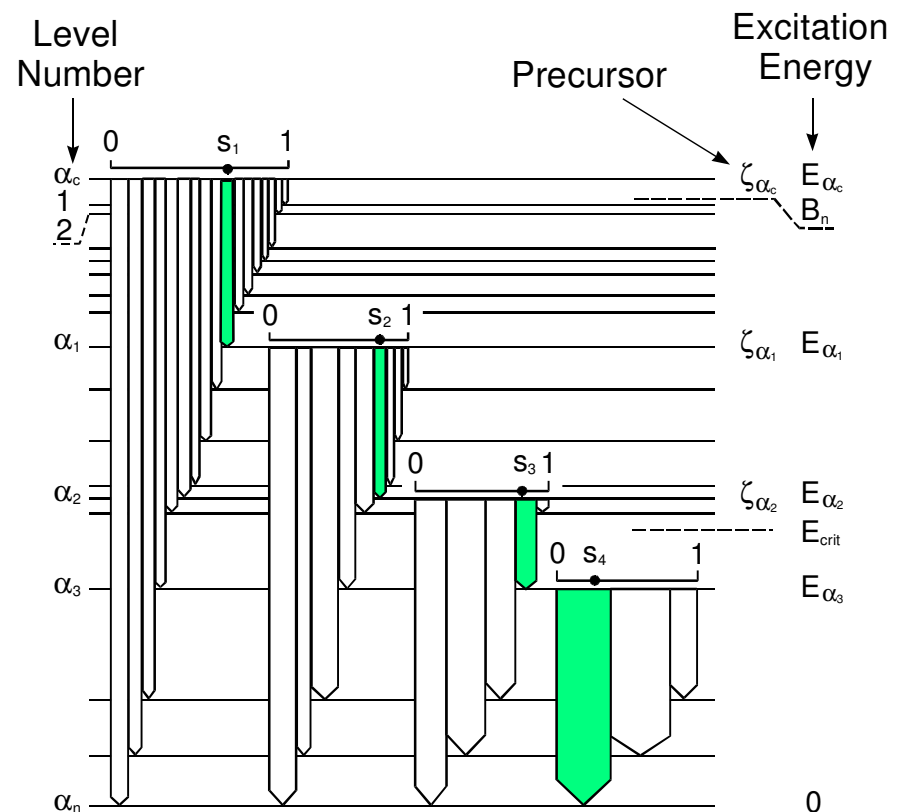
Modelling within ESM

Simulation of the decay:

- “nuclear realization”
(10^6 levels $\Rightarrow 10^{12} \Gamma_{\lambda\gamma^f}$)
 \Rightarrow “precursors” are introduced
- fluctuations originating from nuclear realizations cannot be suppressed

Outcomes from modelling are compared with experimental data

Deterministic character of random number generators is exploited



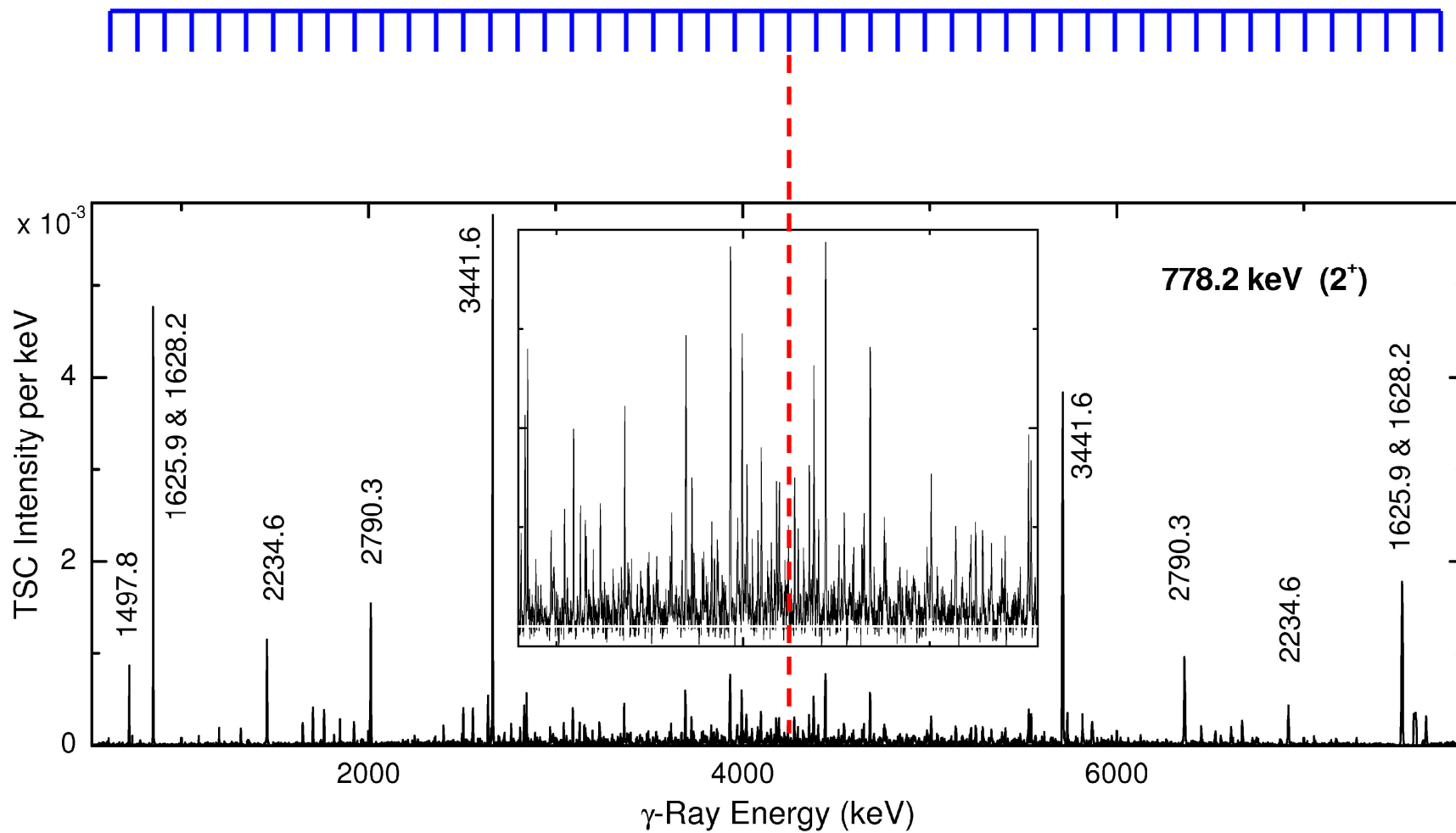
Main feature of DICEBOX

- There exists infinite number of artificial nuclei (nuclear realizations), obtained with the same set of level density and γ -ray SFs models that differ in exact number of levels and intensities of transitions between each pair of them
 - ⇒ leads to different predictions from different nuclear realizations
- DICEBOX allows to treat predictions from different nuclear realizations
- The size of fluctuations from different nuclear realizations depend on the (observable) quantity - in our case intensity of TSC cascades - and nucleus

- Due to fluctuations only “integral” quantities can be compared
- In principle, simulation of detector response must be applied (very simple in the TSC setup, GEANT simulations for DANCE)

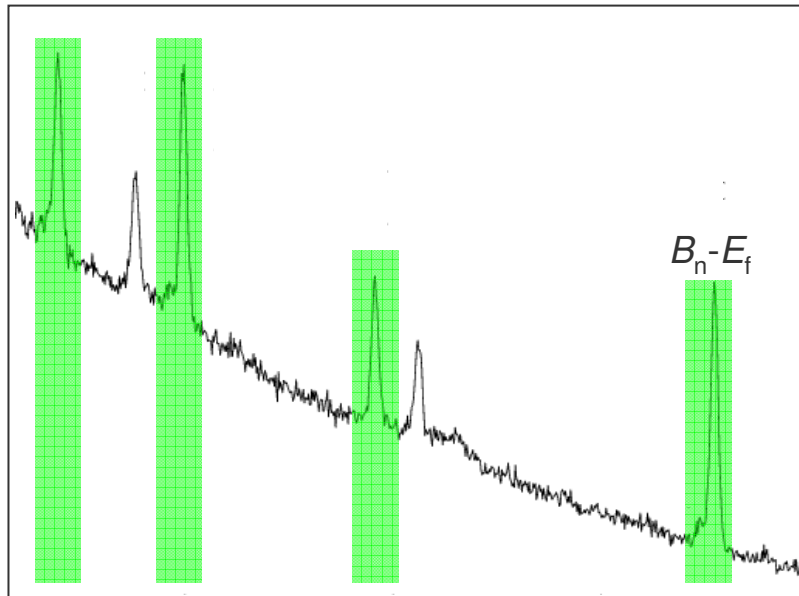
Example of a TSC spectrum

Wide-bin TSC spectra

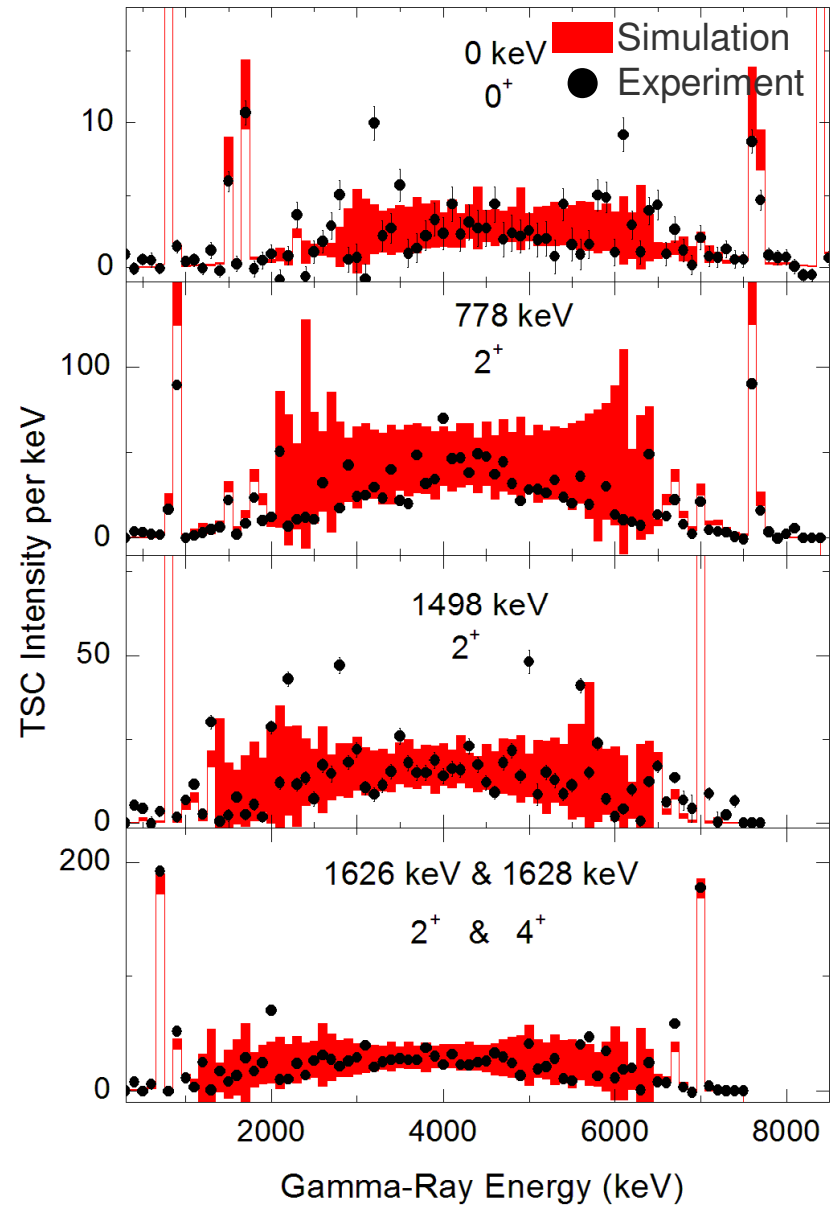


Examples of spectra

Spectrum of energy sums

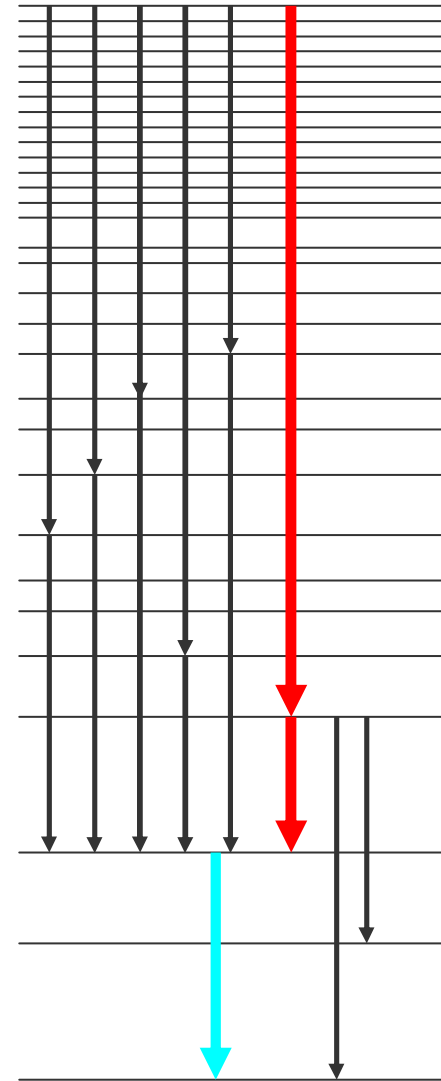


Energy sum $E_{\gamma 1} + E_{\gamma 2}$

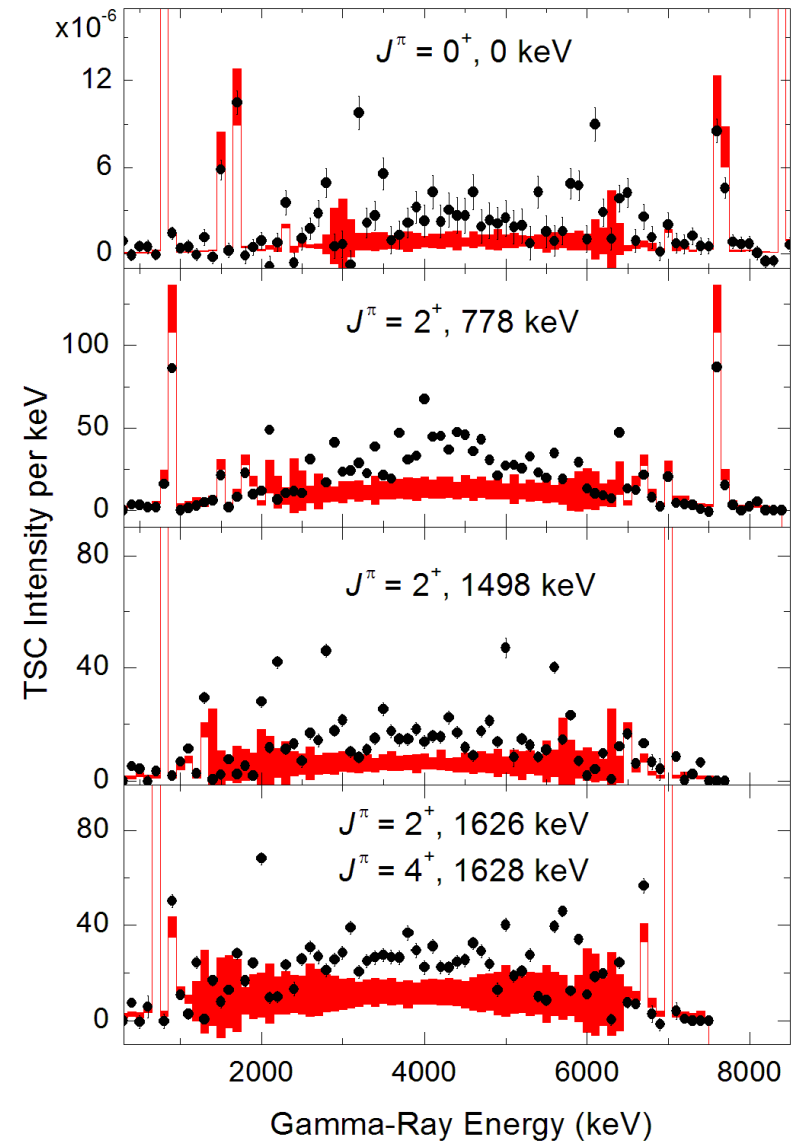
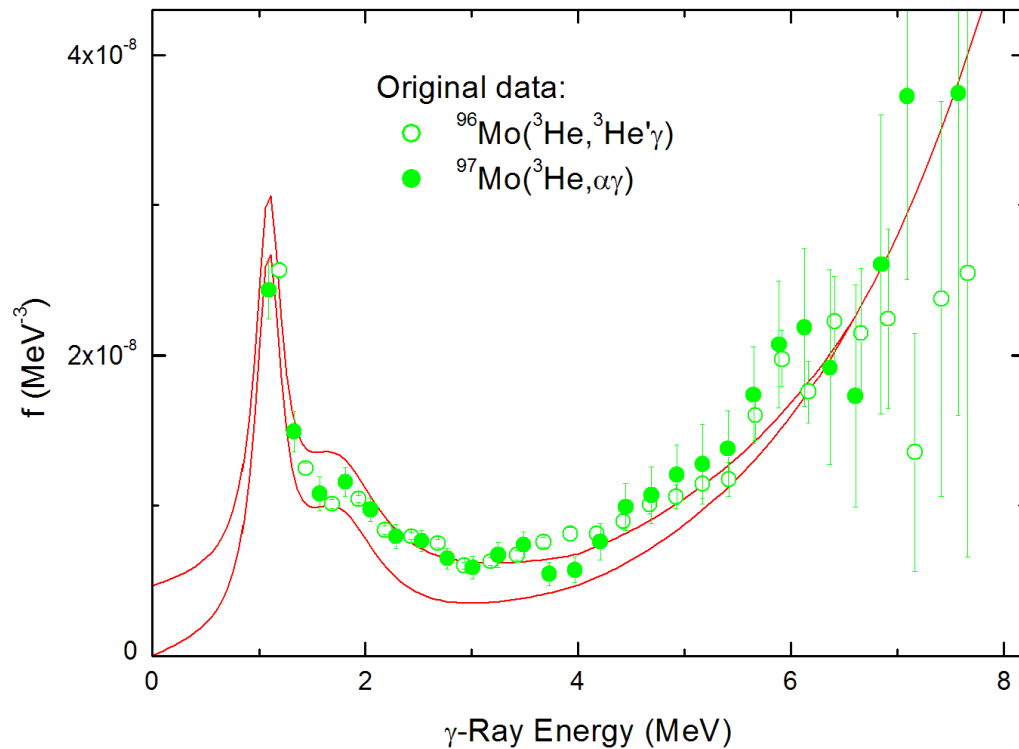


Normalization of experimental spectra

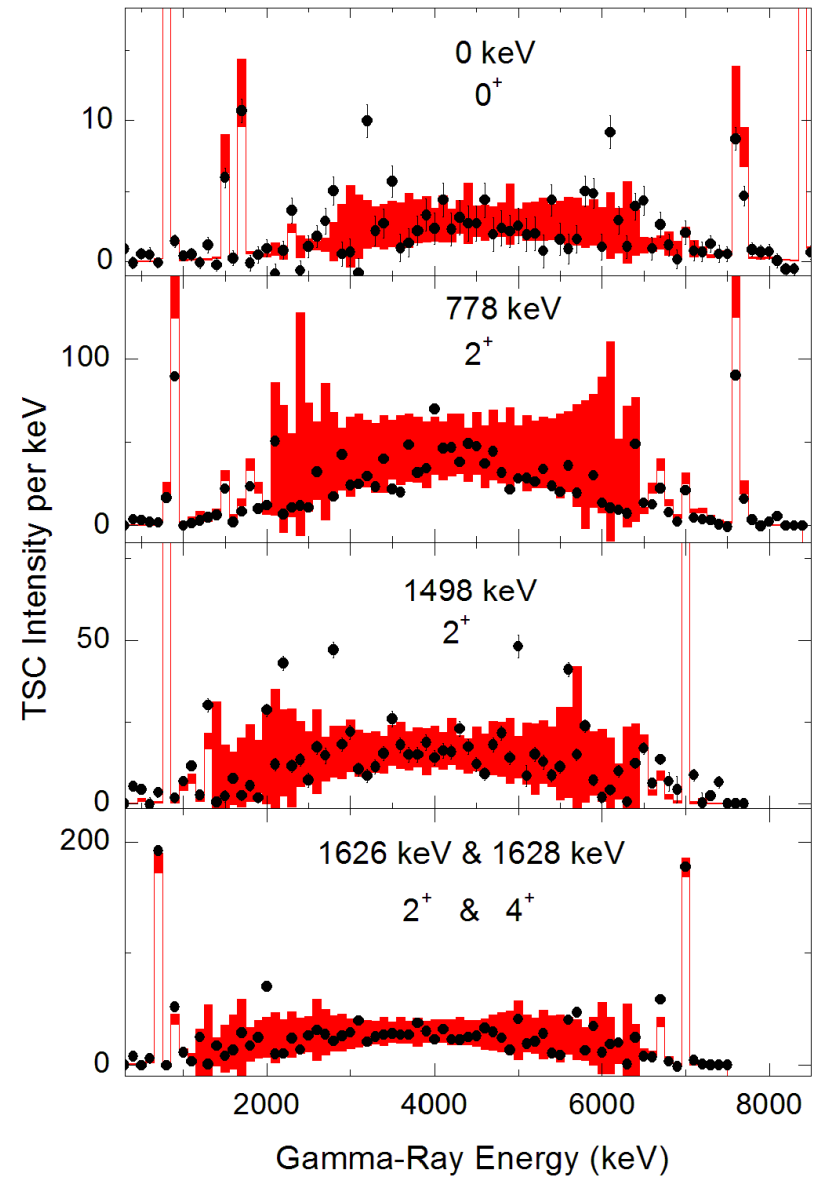
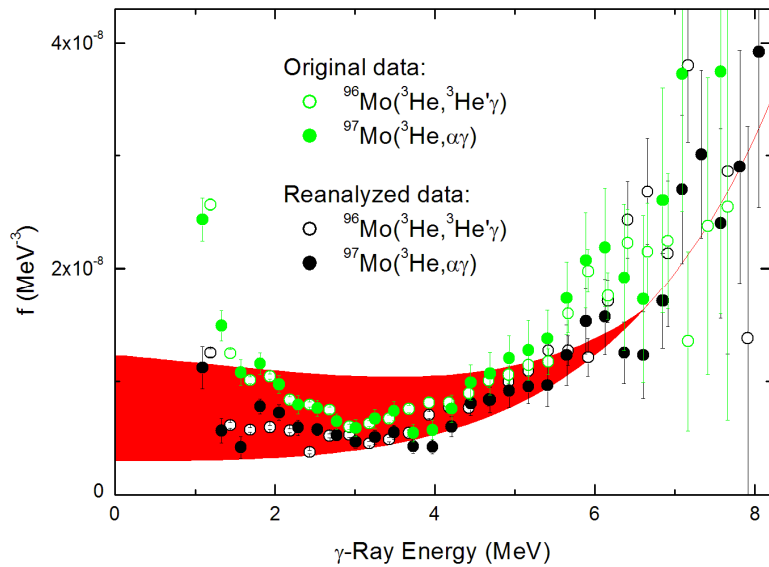
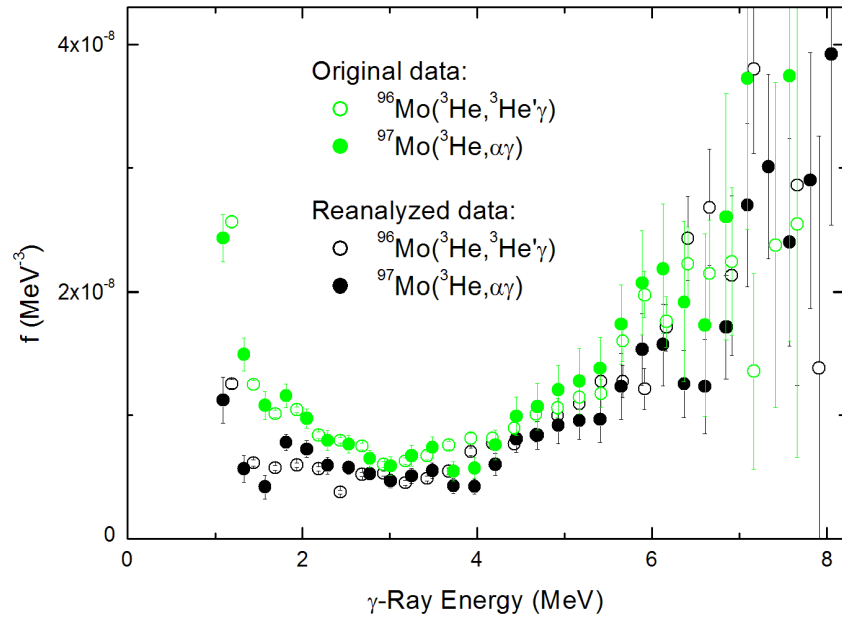
- Knowing intensity of one γ -ray cascade \Rightarrow simulated/experimental TSC intensities to all final levels can be normalized
- Corrections to angular correlation and vetoing must be done



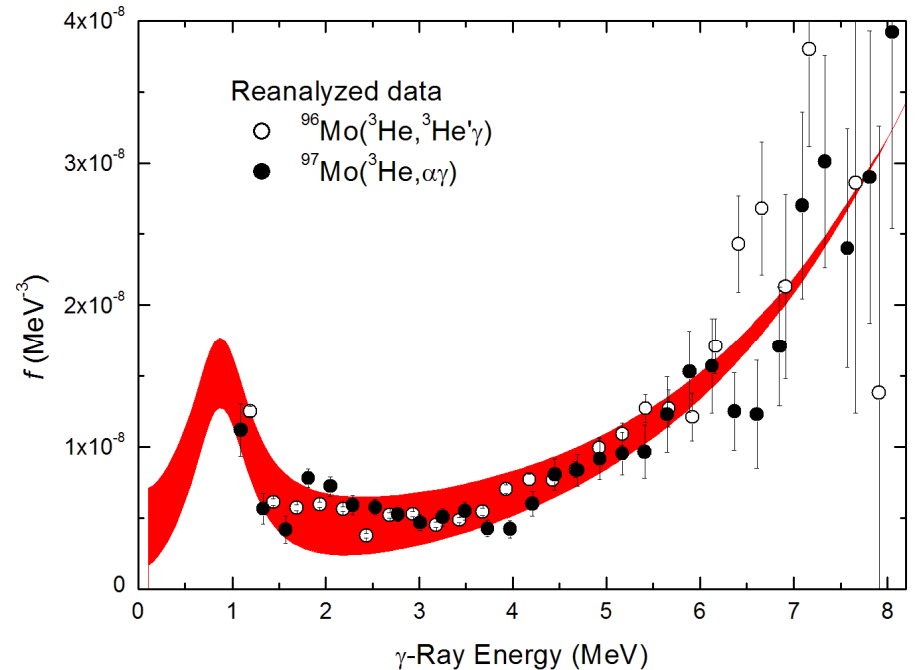
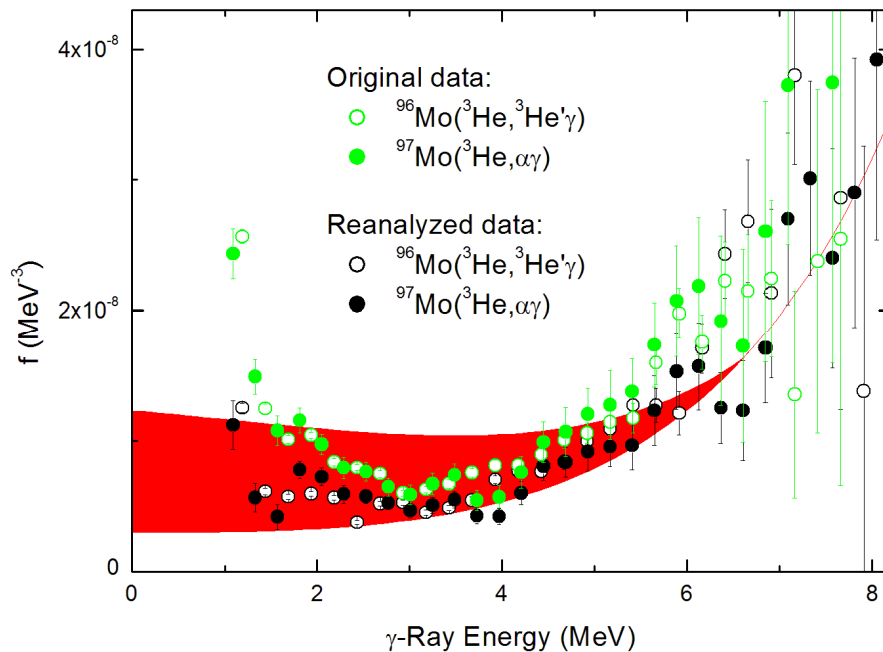
Enhanced PSF at low energies - ^{96}Mo



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Enhanced PSF at low energies - ^{96}Mo

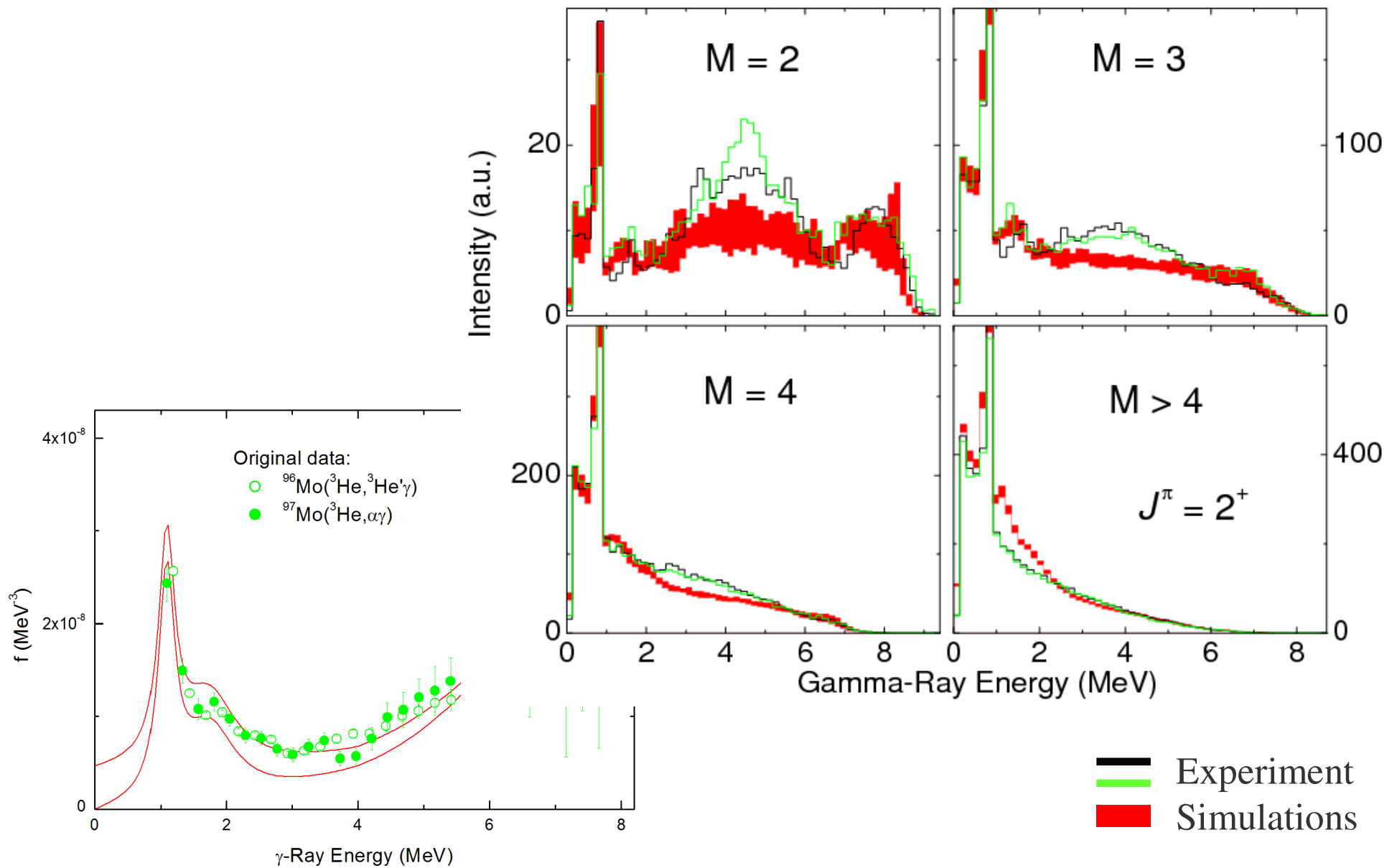


Pictures with comparison similar but correct statistical analysis excludes also this model at 99.8 % confidence level

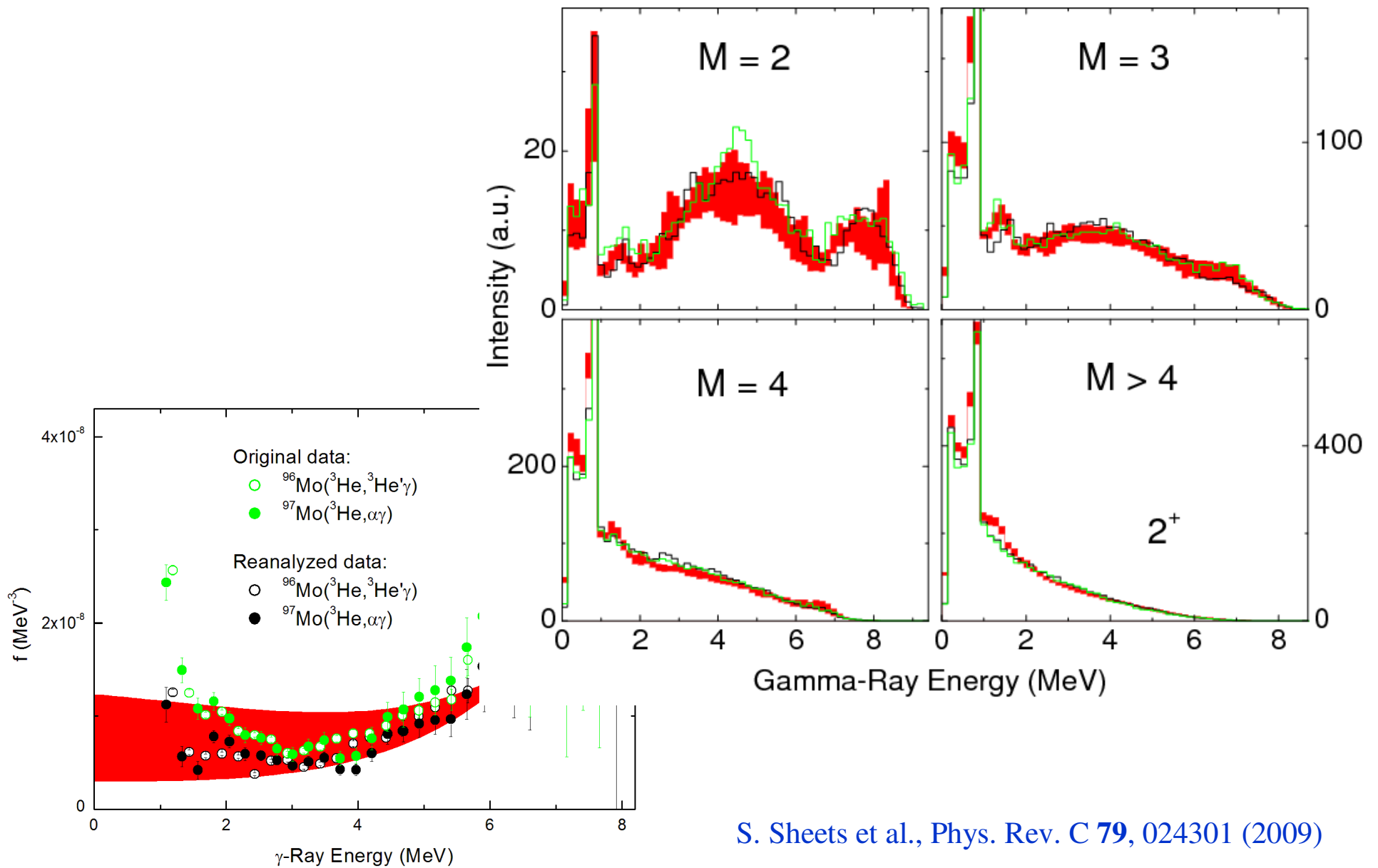
[Krticka et al., PRC 77 054319 \(2008\)](#)

\Rightarrow the enhancement is very weak if any analysis of data from DANCE confirm this

Enhanced PSF at low energies - ^{96}Mo

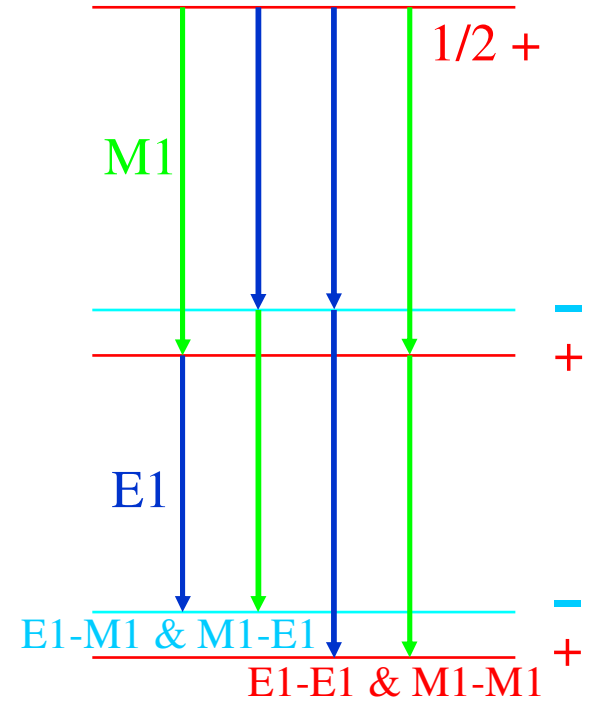
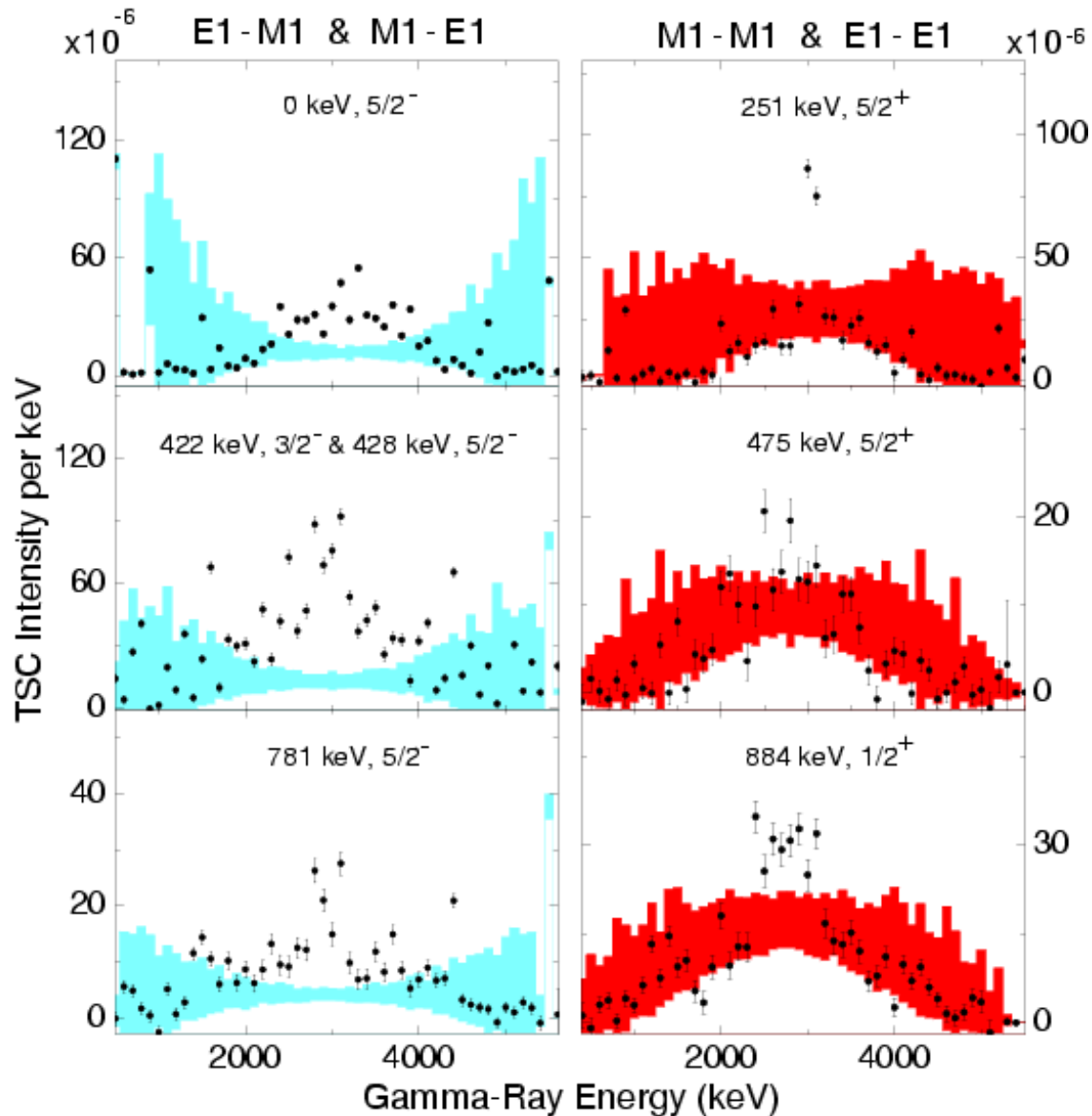


Enhanced PSF at low energies - ^{96}Mo



S. Sheets et al., Phys. Rev. C **79**, 024301 (2009)

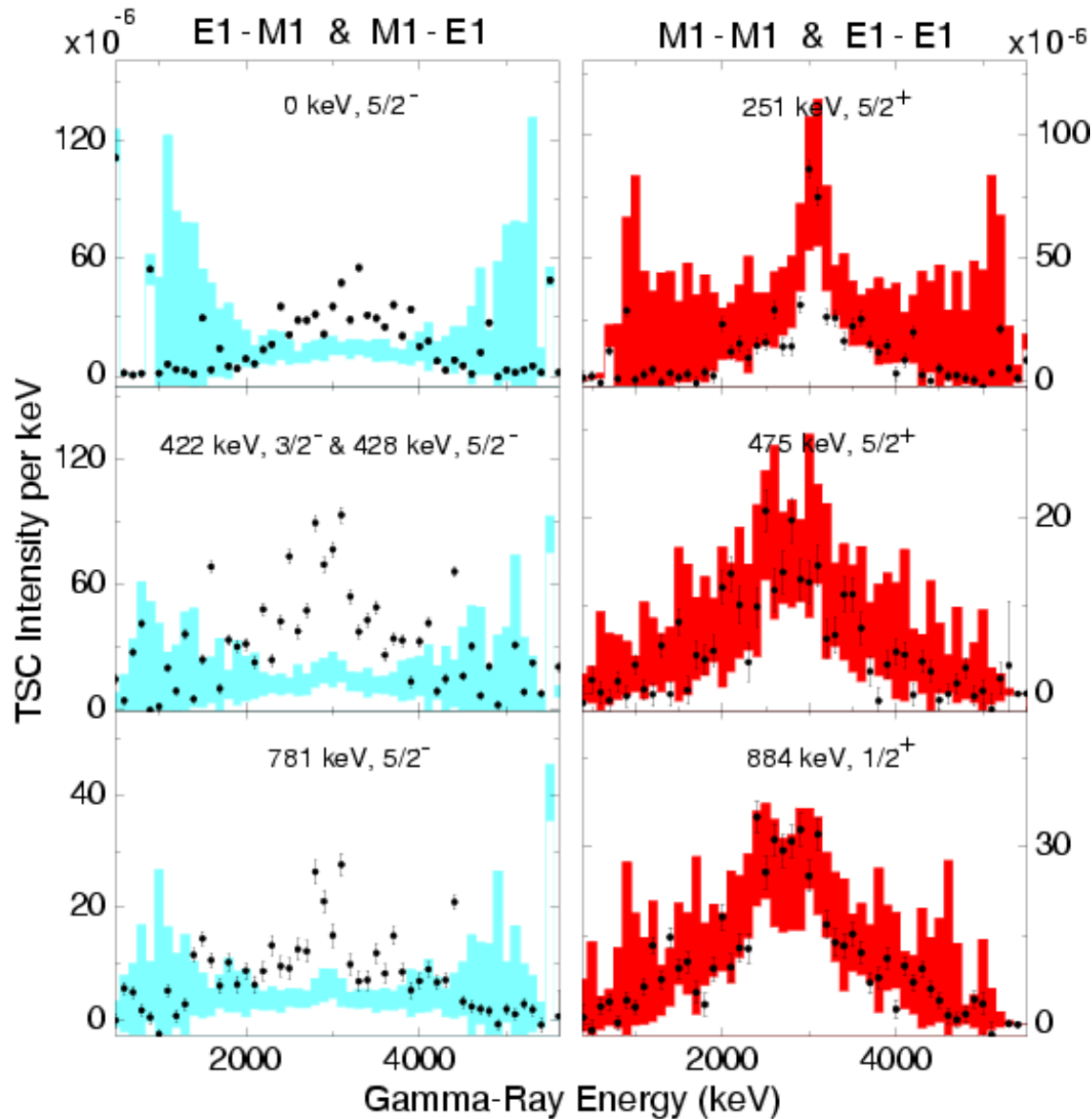
TSCs in the $^{162}\text{Dy}(n,\gamma)^{163}\text{Dy}$ reaction – deformed nuclei



- Řež experimental data
- $\pi_f = +$ } DICEBOX Simulations
- $\pi_f = -$ }

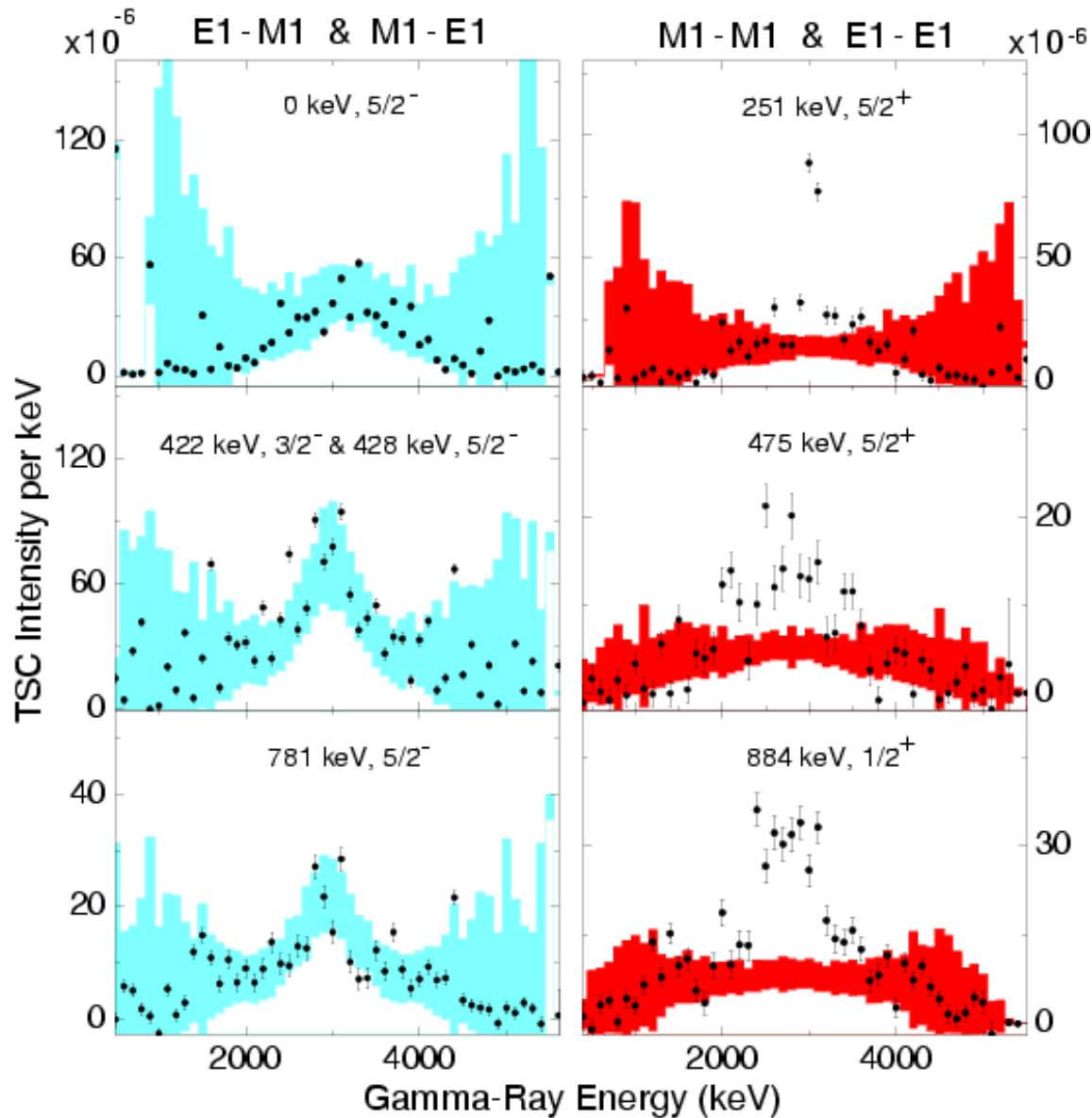
Entire absence of SRs is assumed

TSCs in the $^{162}\text{Dy}(n,\gamma)^{163}\text{Dy}$ reaction



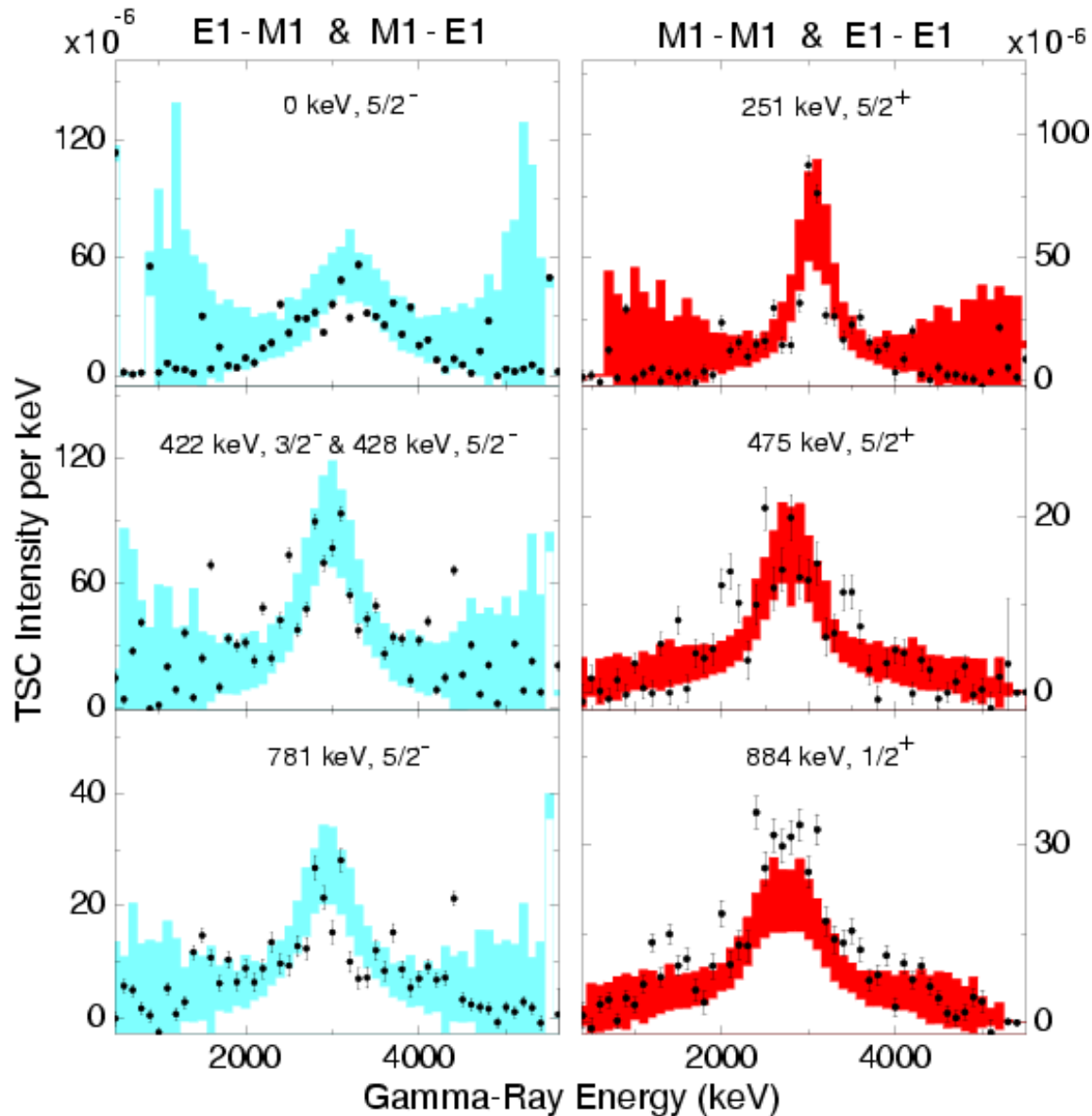
A "pygmy E1 resonance" with energy of 3 MeV assumed to be built on all levels

TSCs in the $^{162}\text{Dy}(n,\gamma)^{163}\text{Dy}$ reaction



SRs assumed to be built only on all levels below 2.5 MeV

TSCs in the $^{162}\text{Dy}(n,\gamma)^{163}\text{Dy}$ reaction



Scissors resonances assumed to be built on all ^{163}Dy levels

$$E = 3.0 \text{ MeV}$$

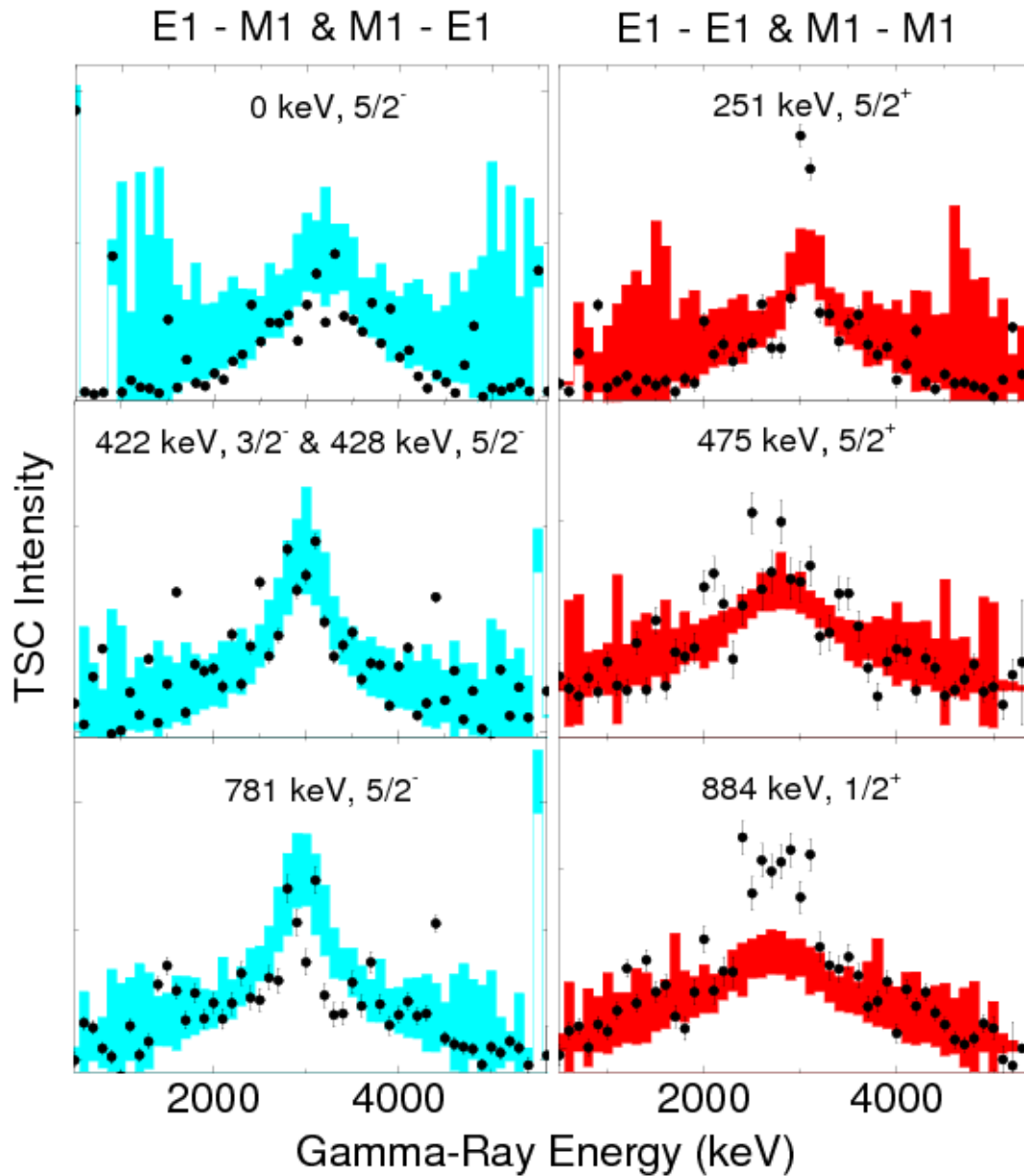
$$\Gamma = 0.6 \text{ MeV}$$

$$\Sigma B \approx 6.2 \mu_N^2$$

M. Krlicka et al.

Phys. Rev. Lett. **92** (2004) 172501

TSCs in the $^{162}\text{Dy}(n,\gamma)^{163}\text{Dy}$ reaction



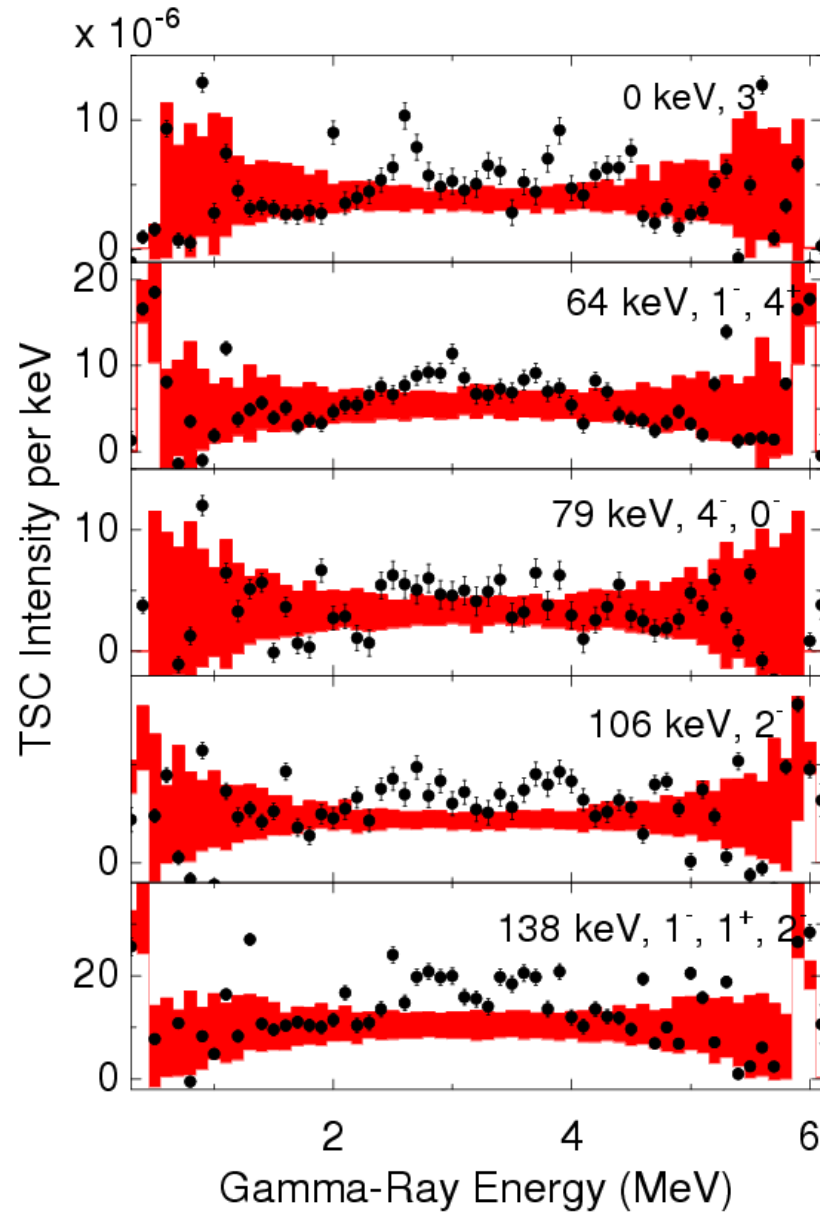
Scissors resonances
assumed to be built
on all ^{163}Dy levels

$$E = 3.0 \text{ MeV}$$

$$\Gamma = 0.6 \text{ MeV}$$

$$\Sigma B \approx 3.0 \mu_N^2$$

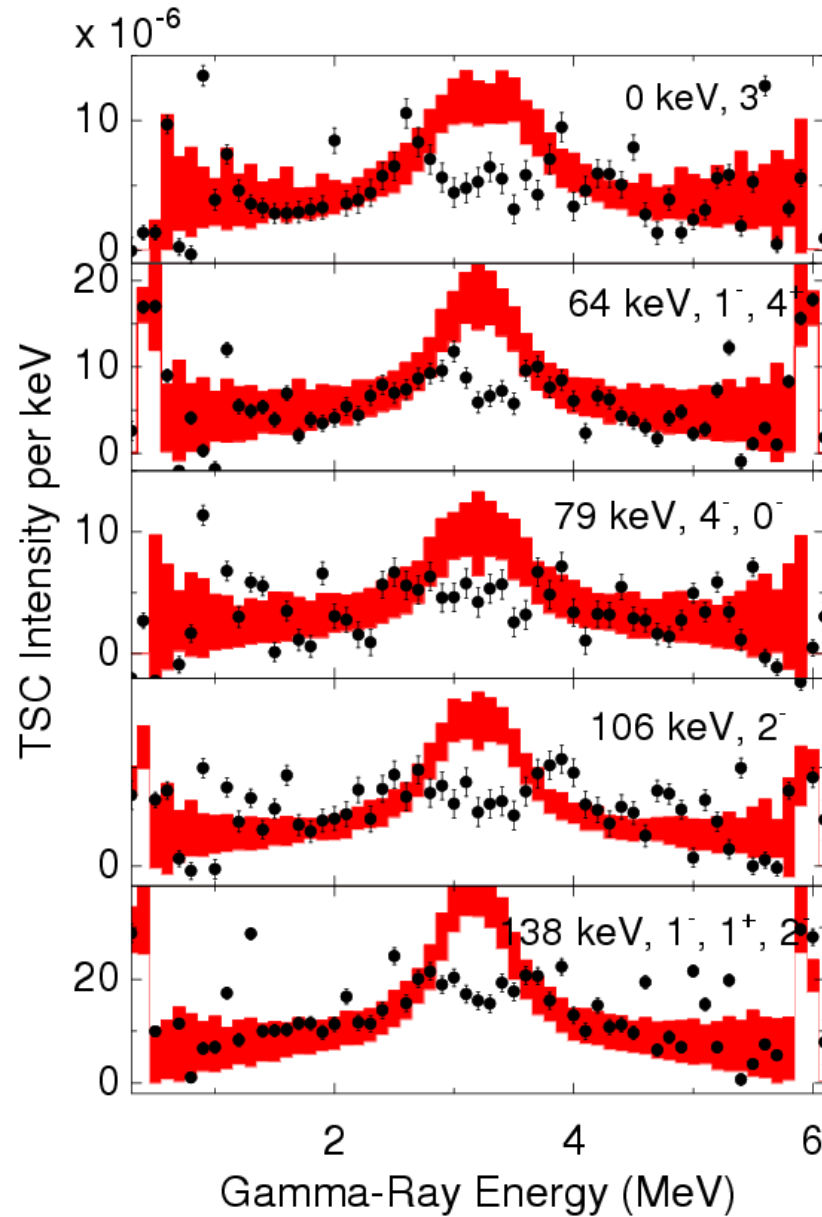
TSCs in the $^{159}\text{Tb}(n,\gamma)^{160}\text{Tb}$ reaction



Preliminary results

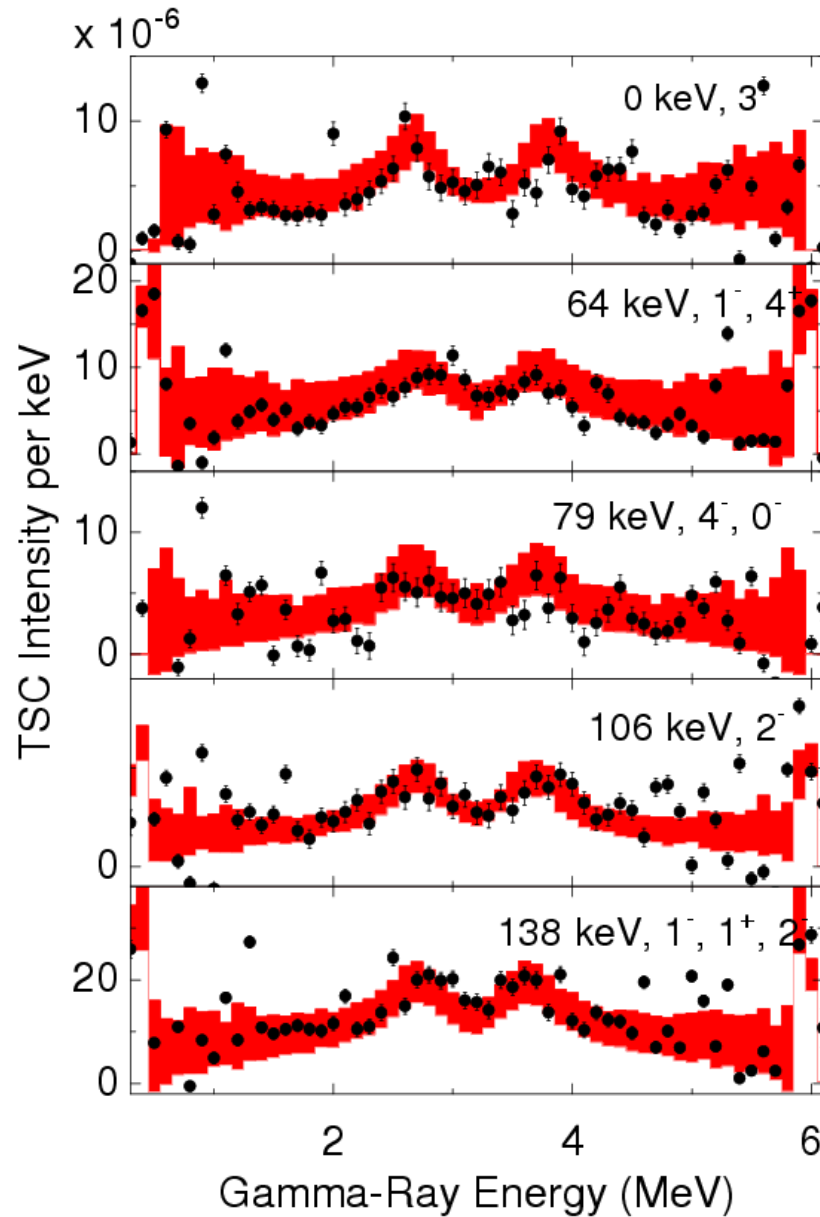
Entire absence
of SRs is assumed

TSCs in the $^{159}\text{Tb}(n,\gamma)^{160}\text{Tb}$ reaction



Scissors mode with
 $E = 3.0 \text{ MeV}$

TSCs in the $^{159}\text{Tb}(n,\gamma)^{160}\text{Tb}$ reaction



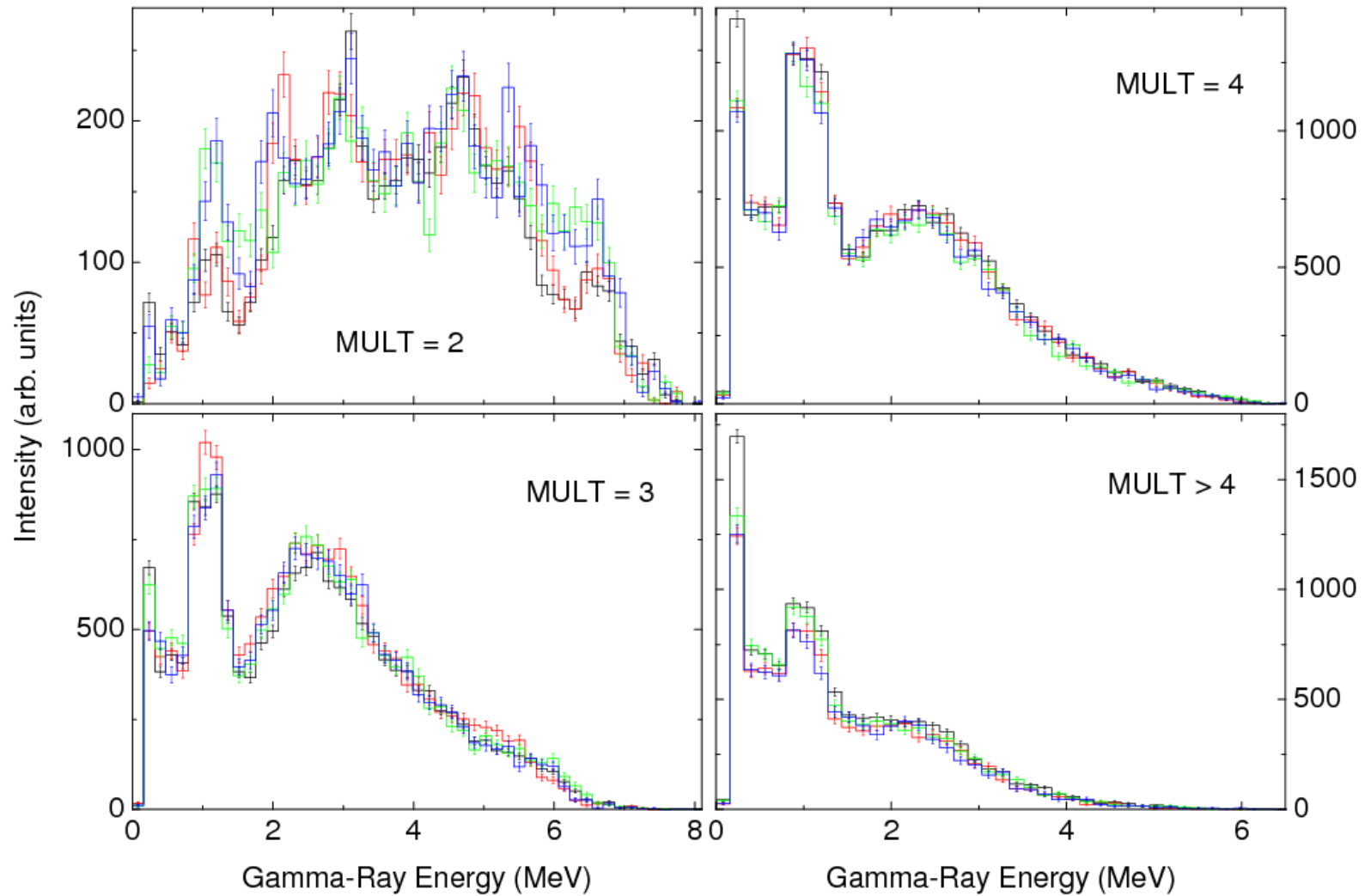
Scissors mode with
 $E = 2.7 \text{ MeV}$
 $\Sigma B \approx 3 \mu_N^2$

Very similar results
also for
 $E = 3.5 \text{ MeV}$
 $\Sigma B \approx 2-7 \mu_N^2$

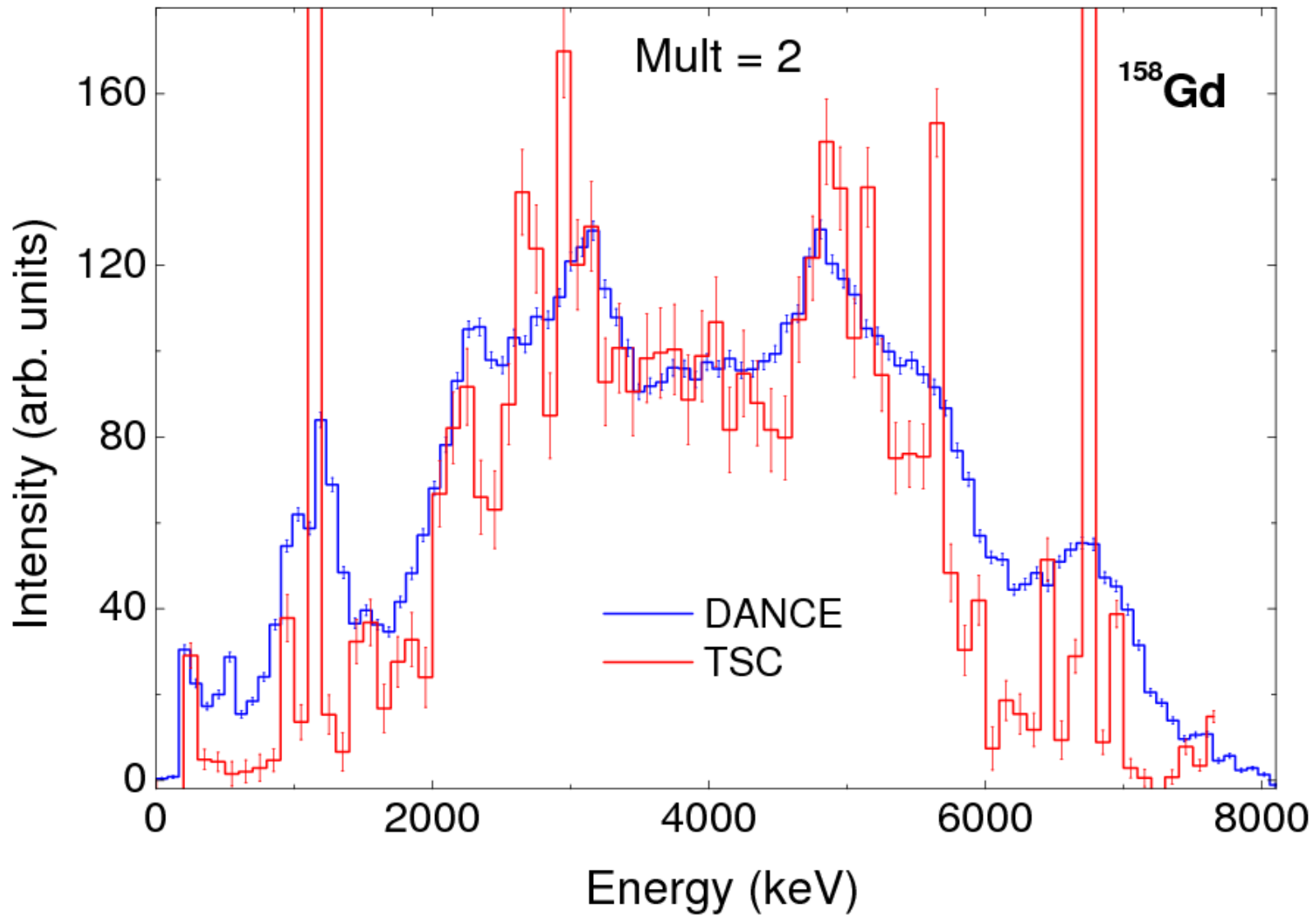
J. Kroll, *diploma thesis*, Prague 2009

$^{157}\text{Gd}(n,\gamma)^{158}\text{Gd}$ reaction – deformed nuclei

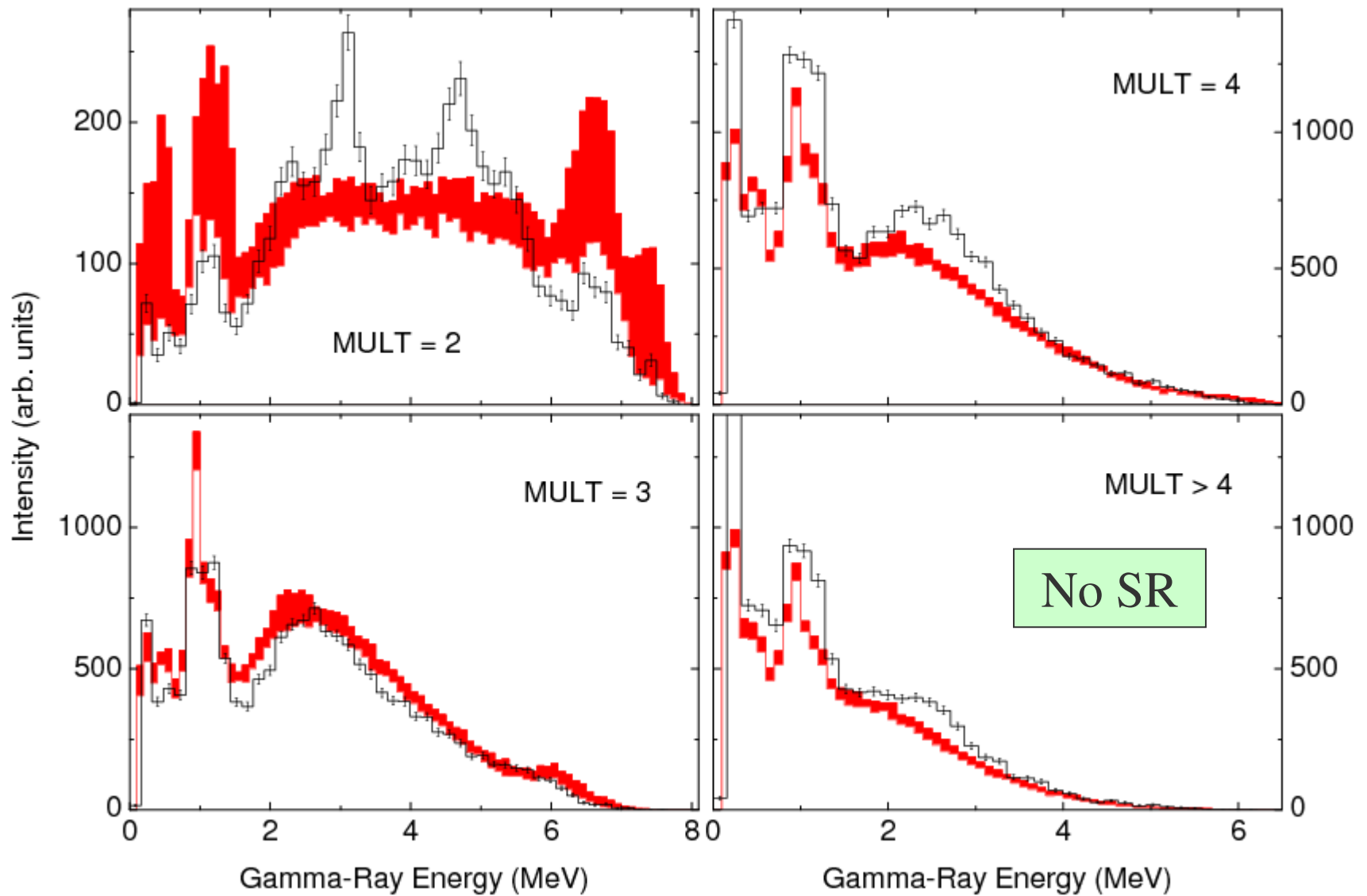
Experimental spectra



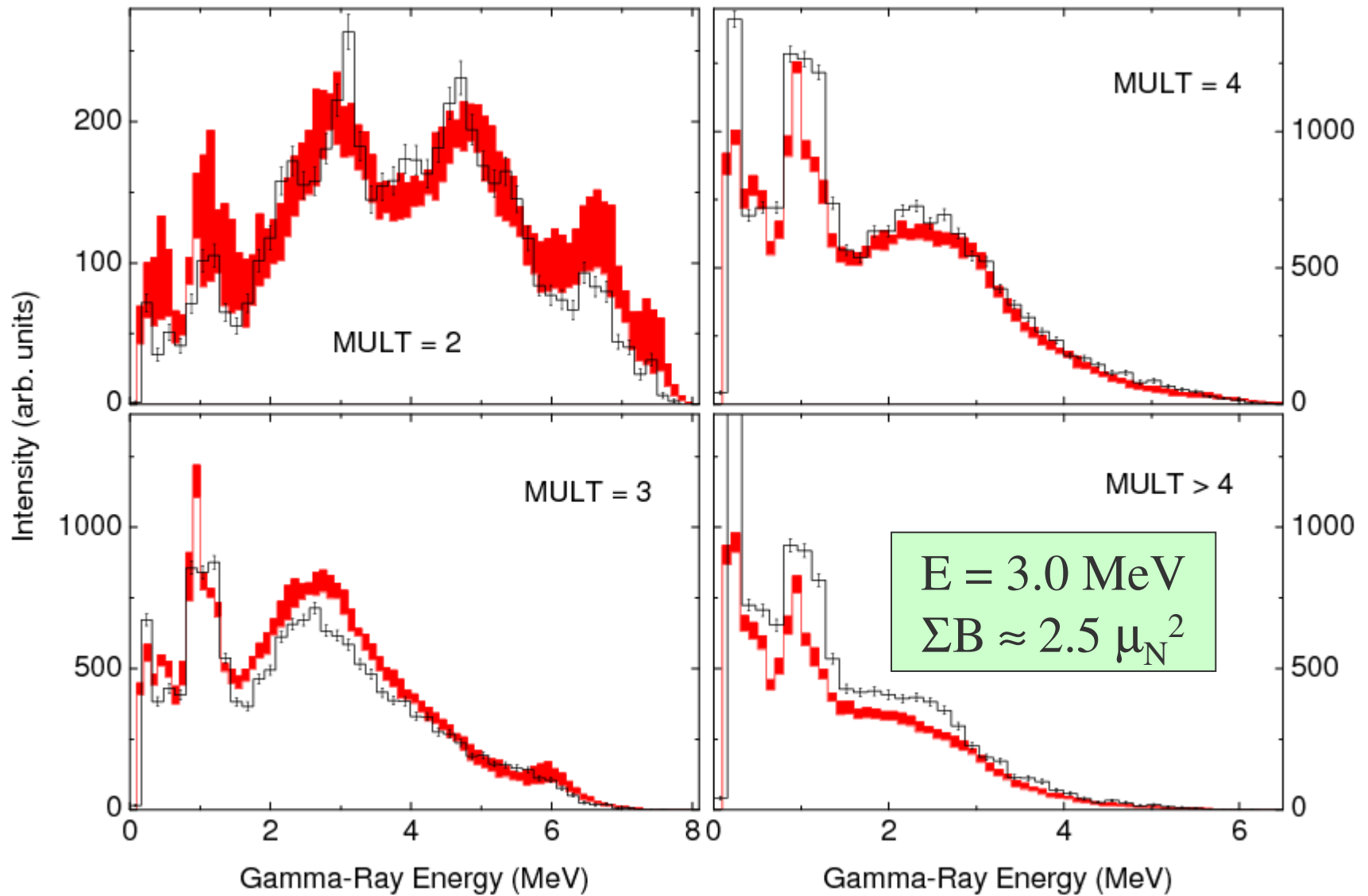
Experiment: TSC vs. DANCE



$^{157}\text{Gd}(n,\gamma)^{158}\text{Gd}$ reaction – deformed nuclei

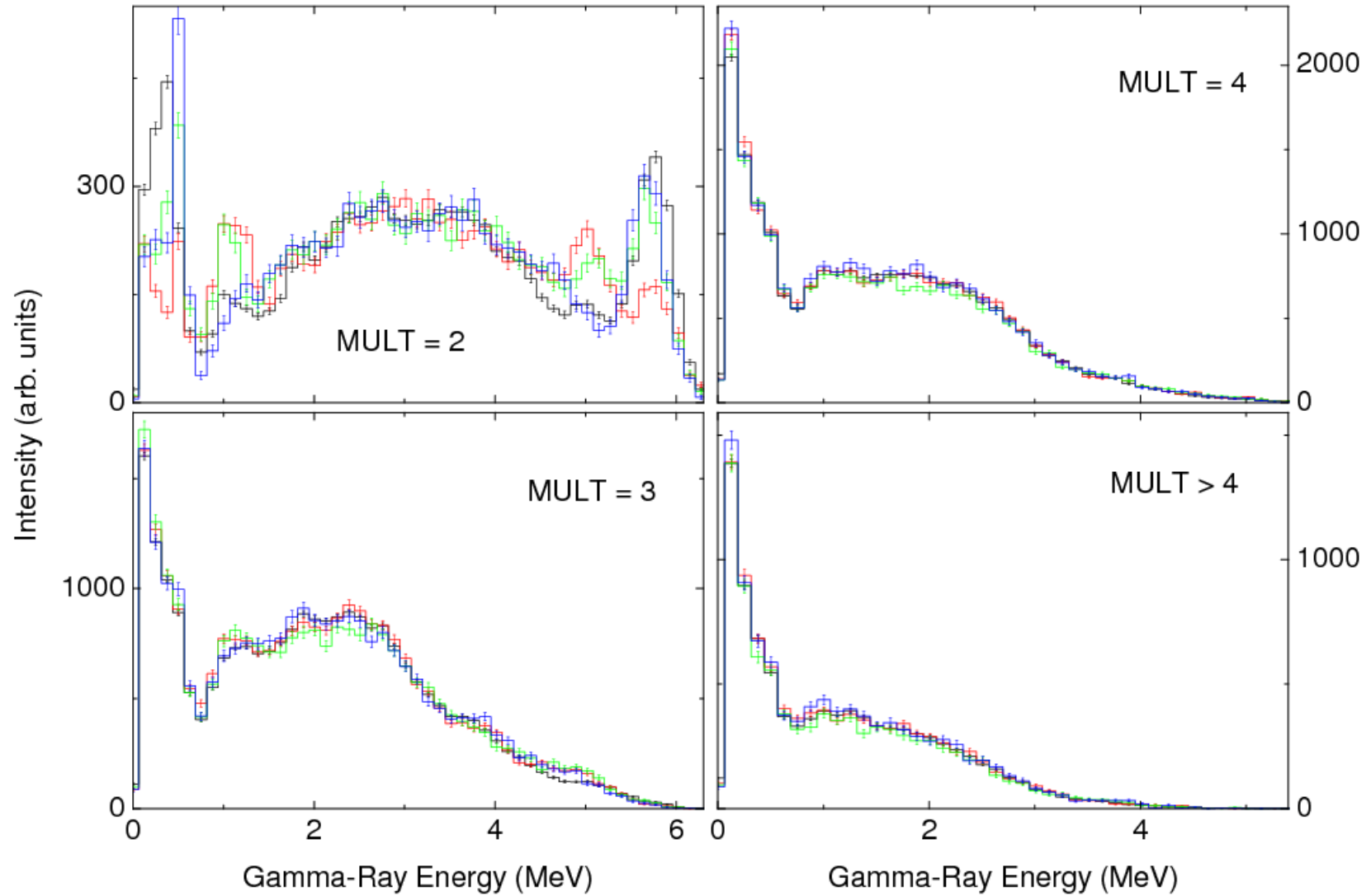


$^{157}\text{Gd}(n,\gamma)^{158}\text{Gd}$ reaction

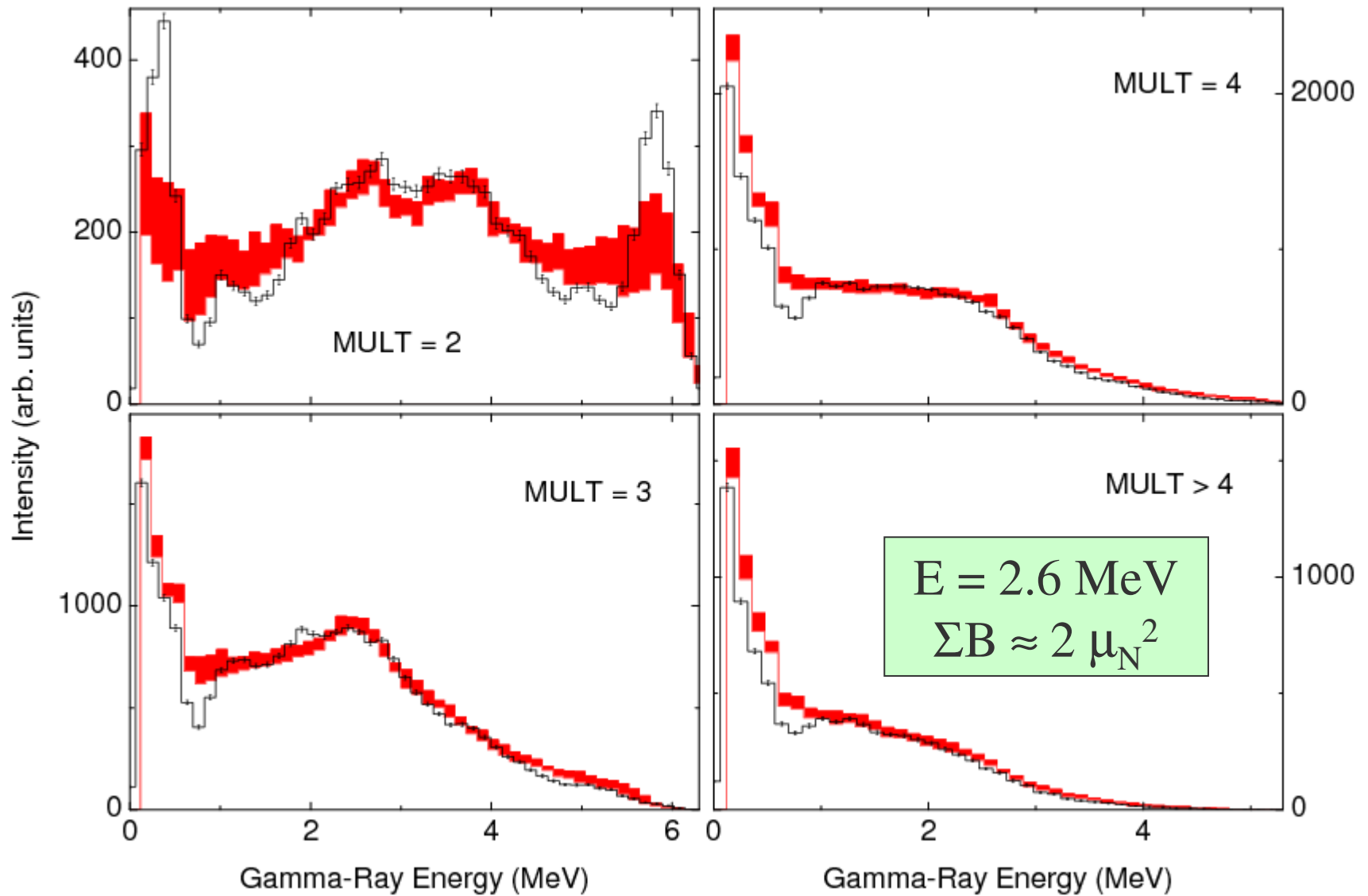


$^{154}\text{Gd}(n,\gamma)^{155}\text{Gd}$ reaction

Experimental spectra



$^{154}\text{Gd}(n,\gamma)^{155}\text{Gd}$ reaction



Conclusions

- Two-step and multi-step γ cascade methods are very powerful tools for studying γ -ray SF
- Spectra from presented experiments cannot be processed without simulations – DICEBOX code allows to keep inherent uncertainties due to statistical character of the decay under control

TSC measurements

Prague - F. Bečvář, M. Krtička, J. Kroll

Řež - I. Tomandl

DANCE

LANL - T.A. Bredeweg, R. Haight, J.M. O'Donnell,
R.S. Rundberg, J.L Uhlmann, D. Vieira, J.M. Wouters,
J.B. Wilhelmy, A. Chyzh, B. Baramsai

LLNL - U. Angvaanluvsan, J.A. Becker, W. Parker, C.Y. Wu,
D. Dashdorj

NCSU - G.E. Mitchell

Prague - F. Bečvář, M. Krtička

Dubna - E.I.Sharapov



**Thank you
for your attention**